

MATH 406 – HOMEWORK VIII

(due Friday 17 April 2009)

1. Assume that $\text{ord}_n a = k$ and that $d|k$. Show that there is some b with $\text{ord}_n b = d$.
2. Suppose that \bar{r} is an inverse of r modulo n . Show that $\text{ord}_n r = \text{ord}_n \bar{r}$.
3. Show that 20 has no primitive roots.
4. Find all primitive roots of 18. Explain carefully, and express your answers as least positive residues. Show all necessary calculations – you do not need a calculator.
5. How many incongruent roots does $x^3 + 12$ have modulo 13? Explain carefully.

NOTE: Explain your work clearly. Your solutions must include enough detail to justify your conclusions.