

MATLAB Log 1, Math 461

```
>> A = [ 2 7 3 0 ; -1 1 2 4; 3 4 6 -2 ]
```

```
A =
```

```
     2     7     3     0
    -1     1     2     4
     3     4     6    -2
```

```
>> A(1,:)
```

```
ans =
```

```
     2     7     3     0
```

```
>> A(2,:) = A(2,:) + 0.5*A(1, :);
```

```
>> A(3,:) = A(3,:) + (-1.5)*A(1,:)
```

```
...
```

```
    2.0000    7.0000    3.0000         0
         0    4.5000    3.5000    4.0000
         0   -6.5000    1.5000   -2.0000
```

```
>> A(3,:) = A(3,:) + (6.5/4.5)*A(2,:);
```

```
>> A(1,:) = A(1, :)/A(1,1) ; A(2,:) = A(2, :)/A(2,2)
```

```
>> A(3,:) = A(3, :)/A(3,3)
```

A =

1.0000	3.5000	1.5000	0
0	1.0000	0.7778	0.8889
0	0	1.0000	0.5763

>> A(1,:) = A(1,:) - A(2,)*3.5 ;

A =

1.0000	0	-1.2222	-3.1111
0	1.0000	0.7778	0.8889
0	0	1.0000	0.5763

>> A(1,:) = A(1,:) + (11/9)*A(3,:) ;

>> A(2,:) = A(2,:) - (7/9)*A(3,:)

A =

1.0000	0	0	-2.4068
0	1.0000	0	0.4407
0	0	1.0000	0.5763

Previous example shows **elementary row-operations** to reduce first to **row echelon form**, then to **reduced row echelon form** resulting in *unique solution*.

MORE GENERALLY: row-echelon form might have final appearance (* means **nonzero** value)

$$\begin{pmatrix} * & a_{12} & a_{13} & \cdots & a_{1k} & b_1 \\ 0 & * & a_{23} & \cdots & a_{2k} & b_2 \\ \cdots & & & & & \\ 0 & 0 & 0 & 0 & 0 & * \end{pmatrix}$$

showing **Inconsistency** (NO SOLUTION), or

$$\begin{pmatrix} * & a_{12} & a_{13} & \cdots & a_{1,n} & \cdots & b_1 \\ 0 & * & a_{23} & \cdots & a_{2,n} & \cdots & b_2 \\ \cdots & & & & & & \\ 0 & 0 & 0 & \cdots & * & * & b_n \end{pmatrix}$$

with number of **pivot positions** less than number of variables *with at least some nonzero coefficients for the extra variables in the final row indicating* (INFINITELY MANY SOLUTIONS)