

# Design of Sample Surveys which Complement Observational Data to Achieve Population Coverage

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# Disclaimer

This report is released to inform interested parties of ongoing research and to encourage discussion of work in progress. The views expressed are the author's and not necessarily the Census Bureau's.

# Observational Versus Survey Data

In future: observational  $\left\{ \begin{array}{l} \text{administrative} \\ \text{web-search} \\ \text{web opt-in} \end{array} \right\}$  data collection

will play a large role in statistical agencies' operations

**Question:** if agencies continue to publish data with assessments of variability, quality and coverage, then what statistical methodology can support probability sampling and combined analysis of survey and observational data ?

**Key is joint modeling of inclusion/response indicators for observational list and sample survey**

## Notes on Data Definitions

- (a) 'Inclusion' for admin-rec list requires record-linkage; models needed for linkage errors in terms of covariates not used in linkage
- (b) Frames (e.g., Census Master Address File) not error-free; Models needed for unit frame errors in terms of covariates  $X_i$
- (c) Sample, linkage indicators for units (persons or Households)

frame	admin. list	sample	respondent
$I_{[i \in \mathcal{U}]}$	$A_i$	$I_{[i \in \mathcal{S}]}$	$R_i$

$R_i$  pseudorandomization defined for  $i \in \mathcal{U}$ , observed for  $i \in \mathcal{S}$

- (d) *Assume same values for covariates & outcomes observed both in admin list & survey*

# Application of Joint Inclusion Model to Survey Design

How to design supplemental surveys if we have a strong model  $p(R_i | A_i = a, X_i, Y_i)$ ,  $a = 0, 1$  ?

If  $\mathcal{A} \subset \mathcal{U}$ , and  $\mathcal{A}^c$  accessible, sample on  $\mathcal{A}^c$  with inclusion probabilities  $\pi_i = \pi_i(X_i)$  and estimate  $Y$ -totals by

$$\sum_{i \in \mathcal{A}} Y_i + \sum_{i \in \mathcal{A}^c \cap \mathcal{S}} R_i Y_i / \{\pi_i p(R_i | A_i = 0, X_i, Y_i)\}$$

or by GREG variants. Weights  $w_i = 1/\pi_i(X_i)$  freely chosen: to minimize variability of  $w_i/p(R_i | A_i = 0, X_i, Y_i)$ .

# Idealized Data Structure

Generally: geographic covariates  $X_i$  observable for all  $i \in \mathcal{U}$

Other covariates  $V_i$  and outcomes  $Y_i$  generally observable only for Admin Rec list  $\mathcal{A}$  units **or** survey/census respondents

**Assume**  $\mathcal{U}$  covers all residential addresses,  $\mathcal{A} \subset \mathcal{U}$

$$\mathcal{D} = \left\{ A_i, X_i, I_{[i \in \mathcal{S}]} \cdot (1, R_i), (A_i + (1 - A_i) R_i \cdot I_{[i \in \mathcal{S}]}) \cdot (V_i, Y_i) \right\}_{i \in \mathcal{U}}$$

$A_i, R_i$  dependent given  $\mathcal{S}$ , and  $Y_i$  dependent on both

Initially assume no  $V_i$  is present

# Joint Models for Indicators & Outcomes

- (1) **Missing-at-Random (MAR)**:  $R_i, Y_i$  (maybe also  $A_i$ )  
indep. given  $X_i$  as in capture-recapture (Alho 1990)
- (2) **NMAR** variants, e.g. logistic regression for  $R_i$  on  $X_i, Y_i$   
and  $A_i$  terms (as in Robins & Rotnitzky 1994)
- (3) **Log-linear models for categorical  $R_i, Y_i, A_i, X_i$**  ; suppressed interactions as in Darroch et al. (1993) *triple system*
- (4) **ANOVA** for  $Y_i$  in terms of  $A_i, R_i$  factors, linear in  $X_i$   
[idea of Prentice et al. (2006) for outcome log-hazards]
- (5) **mixture model for  $R_i, A_i$  given  $X_i$** , as below

# Specific Simulation Model

Consider scalar (continuous)  $X_i$ , 12-dim model for illustration:

**(A.1)** (*SRS or Poisson sampling*)

**(A.2)** (*Mixture propensities*) (idea from education statistics)

$(A_i, R_i)$  dist'n mixture of indep. & degenerate  $A = R = 1$ :

$$P(A_i = j, R_i = k | X_i) = \gamma(X_i) I_{[j=k=1]} +$$

$$(1 - \gamma(X_i)) a(X_i)^j (1 - a(X_i))^{1-j} r(X_i)^k (1 - r(X_i))^{1-k}$$

**(A.3)** (*ANOVA outcome, factors  $A_i, R_i$* )

$$Y_i = \alpha_0 + \alpha_1 X_i + (\alpha_2 + \alpha_3 X_i) \cdot R_i + (\alpha_4 + \alpha_5 X_i) \cdot A_i + \epsilon_i$$

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$$\gamma(x) \equiv \gamma, \quad a(x) = \text{plogis}(\theta_1 + \theta_2 x), \quad r(x) = \text{plogis}(\beta_1 + \beta_2 x)$$



# Simulation Objectives

- illustrate feasibility of estimation
- illustrate information due to **joint** model for indicators
- illustrate estimation errors based on MAR model

Begin with  $N = 10^4$ ,  $n = 500$ :

Logistic regression coeff's  $\underline{\theta}, \underline{\beta}$  & mixture  $\gamma$ :

ML scores preferred to EM which is too slow

Parameters  $\underline{\alpha}$  not estimated here, could use least-squares

$$Y \sim \begin{cases} (1, X, R, RX, A, AX) & \text{on } \mathcal{S} \\ (1, X, E(R|X, A = 1), X E(R|X, A = 1)) & \text{on } \mathcal{A} \cap \mathcal{S}^c \end{cases}$$

# Simulation Results

(I) Contrast between estimation accuracy based on  $(A_i, X_i)$  versus  $\mathcal{D} = \{(A_i, X_i, R_i)\}$  data with  $n=500$

Data	$N$	Param	$\theta_1$	$\theta_2$	$\gamma$	$\beta_1$	$\beta_2$
A,X	1e4	True	-0.400	2.500	0.300	0.600	1.600
		Avg	-0.982	2.985	0.405	*	*
		SD	0.448	0.356	0.091	*	*
A,R,X		Avg	-0.586	2.709	0.302	0.601	1.620
		SD	0.226	0.149	0.068	0.272	0.486
A,X	2e5	True	-0.200	1.700	0.200	0.800	1.200
		Avg	0.202	1.556	0.000	*	*
		SD	0.279	0.105	0.160	*	*
A,R,X		Avg	-0.077	1.671	0.139	0.930	1.166
		SD	0.104	0.045	0.233	0.393	0.048

## Additional Results

**(II)** Contrast estimates & precision based on mixture model vs. MAR (conditional independence) model with same form of  $p(A|X)$ ,  $p(R|X)$  ,  $N=10,000$  and  $n=500$ , with  $\mathcal{D}$  data

Model	Stat	$\theta_1$	$\theta_2$	$\gamma$	$\beta_1$	$\beta_2$
True		-0.400	2.500	0.300	0.600	1.600
Correct	Avg	-0.586	2.709	0.302	0.601	1.620
	SD	0.226	0.149	0.068	0.272	0.486
Misspec.	Avg	-0.978	2.982	0.404	0.357	1.703
	SD	0.020	0.015	0.004	0.263	0.516

# Summary & Further Research

- Advocated joint modeling of list & response indicators for admin-records/survey research
- Models similar to capture-recapture coverage estimation, but data are different than those in Census coverage estimation
- Need extensions of models & estimates to realistic data including covariates  $V_i$  observed only within samples or admin recs

Other related research problems:

- (i) record-linkage strengths and accuracy in terms of covariates
- (ii) research on frame accuracy in terms of covariates

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**Thank you !**

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