

### Actuarial Mathematics: Final-Project Topics

The following is a list of *suggested* topics for a 5-page final paper or project in lieu of a final exam in the course. The paper or project will be due no later than the official exam date of Wed., May 19, 2004. The alternative to doing a paper will be a problem set of (about 10–12) past Actuarial Exam problems on the topics of the course.

The paper is to be based on at least one source such as a journal article or textbook, and is to represent some additional reading beyond the assigned reading in the course. It need not be typed.

The list below is not exhaustive: if you think of a different topic you would like to write on, please see me and I'll try to find suitable material on it for you to read.

#### TOPICS

(A) Statistical goodness of fit of a hypothesized ‘theoretical’ lifetime distribution (with or without fitted parameters). This topic would involve reading about  $\chi^2$  goodness-of-fit tests and implementing one on a survival-time data set.

(B) Estimating a survival function with the ‘Kaplan-Meier Estimator’: this is a standard biostatistics topic, extending life-table ideas to the case where some individuals are lost to observation or die from an uninteresting (e.g., accidental) cause.

(C) ‘Graduation’, or numerical interpolation and smoothing of life-table age-specific death-rates. This topic is related to smoothing splines, and would involve implementation using illustrative life-table data.

(D) ‘Leslie matrices’: biological/demographic models of population size, from which one can see whether a small population is likely to die out. (This topic is related to the probability topic of (Multitype) Branching Processes.)

(E) Risk-and-ruin theory, or Reinsurance. This topic involves simulation or mathematical calculations of the probability over some longer time-horizon of disastrous adverse fluctuations in survival which would cause an insurer to go bankrupt.

Of these topics, (A) & (B) are primarily statistical; (C) involves some numerical analysis; (D) involves linear algebra and a little bit of *Markov chain* theory; and (E) involves *either* a little more Markov chain and stochastic-process theory *or* a willingness to learn a little bit about simulating random insurance portfolios on the computer. (In the past, (A)-(C) have been the most popular, with (C) the clear winner.)