# MATH 241 Sections Exam 1 Spring 2021 (JWG) 

## Exam Submission:

1. From the moment you download this exam you have three hours to take the exam and submit to Gradescope. This includes the entire upload and tag procedure so do not wait until the last minute.
2. Tag your problems! Please!
3. You may print the exam, write on it, scan and upload.
4. Or you may just write on it on a tablet and upload.
5. Or you are welcome to write the answers on a separate piece of paper if other options don't appeal to you, then scan and upload.

## Exam Rules:

1. You may ask for clarification on questions but you may not ask for help on questions!
2. You are permitted to use your notes and the textbook. You are permitted to use a calculator for basic arithmetic.
3. You are not permitted to use other resources. Thus no friends, internet, etc.
4. By taking this exam you agree that if you are found in violation of these rules that the minimum penalty will be a grade of 0 on this exam.

## Work Shown:

1. Show all work as appropriate for and using techniques learned in this course.
2. Any pictures, work and scribbles which are legible and relevant will be considered for partial credit.

$$
\begin{aligned}
\text { Point }: & (1,2,3) \\
\text { Line }: & \overline{\boldsymbol{r}}(t)=t \hat{\boldsymbol{\imath}}+(2 t+1) \hat{\boldsymbol{\jmath}}+3 t \hat{\boldsymbol{k}}
\end{aligned}
$$

Find the equation of the plane containing both the point and the line and write it in the form $a x+b y+c z=d$.
2. Show that the set of points in 2D which are equidistant from the points $(2,3)$ [10 pts] and $(8,10)$ form a line and find the parametric vector equation of the line.

$$
\begin{aligned}
\text { Plane }: & x-2 y+z=18 \\
\text { Line }: & \frac{x-1}{2}=y, z=7
\end{aligned}
$$

Show that the line and the plane are parallel and find the distance between them.
4. Given the curve with parameterization:

$$
\overline{\boldsymbol{r}}(t)=t \hat{\boldsymbol{\imath}}+2 \hat{\boldsymbol{\jmath}}+t^{2} \hat{\boldsymbol{k}} \text { for }-1 \leq t \leq 1 .
$$

(a) Sketch the curve. Mark the start and end points with their coordinates.
(b) Is the parameterization closed or not? Justify.
(c) Is the parameterization smooth, piecewise smooth or neither? Justify.
5. Consider the curve and plane given here:

$$
\begin{aligned}
\text { Curve }: & \overline{\boldsymbol{r}}(t)=t^{2} \hat{\boldsymbol{\imath}}+(2 t+3) \hat{\boldsymbol{\jmath}}-t \hat{\boldsymbol{k}} \\
\text { Plane }: & x-2 y+z=18
\end{aligned}
$$

(a) The curve intersects the plane twice. Find the two $t$-values and the two [5 pts] points.
(b) Write down an integral for the distance traveled by the curve between the [5 pts] two intersection points. Do not evaluate.
(c) Determine whether the curve is traveling perpendicular to the plane at [5 pts] either intersection point.
6. Consider the curve with parameterization given here:

$$
\overline{\boldsymbol{r}}(t)=\left(t^{4}+t\right) \hat{\boldsymbol{\imath}}+2 t^{3} \hat{\boldsymbol{\jmath}}-(t+8) \hat{\boldsymbol{k}}
$$

Calculate each of the following:
(a) $\overline{\boldsymbol{v}}(1)$
(b) $\overline{\boldsymbol{a}}(1)$
(c) $\overline{\boldsymbol{T}}(1)$
(d) $a_{\overline{\boldsymbol{T}}}(1)$
(e) $a_{\bar{N}}(1)$
(f) Use (b) through (e) to calculate $\bar{N}(1)$.
7. Find the point on the sphere $(x-1)^{2}+(y+2)^{2}+(z-3)^{2}=16$ which is as far [10 pts] as possible from the point $(3,5,5)$.

