

Math 241 Section 13.3: Partial Derivatives

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1. Definition and Notation

Give a formal definition of the partial derivatives (in terms of limits) and then give the way that we actually do them - treating other variables as constants. We have notation $f_x = \frac{\partial f}{\partial x}$ and $f_y = \frac{\partial f}{\partial y}$.

Examples: Lots of examples, making sure to hit some that involve quotient rules, chain rules, etc.

2. Methods of Visualization:

(a) Talked about how $f_x(x, y)$ gives the slope of the tangent line in the x -direction with y fixed and similarly $f_y(x, y)$ gives the slope of the tangent line in the y -direction with x fixed. This is harder to see for more variables like $f_x(x, y, z)$.

(b) If $f(x, y)$ gives the temperature of the plane at (x, y) then $f_x(x, y)$ give the instantaneous temperature change of an object with respect to distance (for example, degrees Celsius per meter) as it passes through (x, y) in the positive x -direction. Similarly for f_y . This works nicely in 3D too.

Example: Do one with units and explanation.

3. Higher Derivatives

Talk about higher derivatives and especially comment on the notation $f_{xy} = \frac{\partial^2 f}{\partial y \partial x}$, $f_{yx} = \frac{\partial^2 f}{\partial x \partial y}$,

$$f_{xx} = \frac{\partial^2 f}{\partial x^2}, f_{yy} = \frac{\partial^2 f}{\partial y^2}.$$

Example: Do one.

Mentioned that almost always $f_{xy} = f_{yx}$ for example.