

**MATH 246 Groupwork 2.5 & 2.6****Name:** \_\_\_\_\_

1. Find the solution to the initial value problem

$$y'' - y' = 2 - 2t \text{ with } y(1) = 2 \text{ and } y'(1) = -3$$

by following the steps:

- (a) Eyeball a single solution  $Y_P(t)$  to the differential equation. Hint: It's a simple polynomial with one term.
  
  
  
  
  
  
  
  
  
  
- (b) Find a fundamental pair for the associated homogeneous differential equation.
  
  
  
  
  
  
  
  
  
  
- (c) Write down the general solution for the given differential equation.
  
  
  
  
  
  
  
  
  
  
- (d) Find the specific solution to the initial value problem.

2. Using the Method of Undetermined Coefficients, write down the undetermined  $Y_P(t)$  for each of the following. The first is done for you so you know how little you need to do!

(a)  $y'' - 5y' + 6y = t + 1$

Solution:  $Y_P(t) = At + B$

(b)  $y'' - 5y' + 6y = t^2$

(c)  $y'' - 5y' + 6y = te^{2t}$

(d)  $y'' - 5y' + 6y = e^{3t}$

(e)  $y'' - 5y' + 6y = (3t^2 + 1)e^{3t}$

(f)  $y'' - 4y' + 13y = e^{3t} \cos(t)$

(g)  $y'' - 4y' + 13y = te^{2t} \sin(3t)$

3. Find a solution to  $y'' - 5y' + 6y = te^{2t}$  using the Method of Undetermined Coefficients. Note that you did part of this in 2(c).