## MATH310 Groupwork 2022-07-19

## NAME:

1. Prove $\forall a, b, c \in \mathbb{Z}$ if $a$ divides $b-1$ and $a$ divides $c-1$ then $a$ divides $b c-1$.

Solution:
2. Prove there exist integers $m$ and $n$ such that $15 m+9 n=3$.

## Solution:

3. Prove by contradiction that there is no smallest positive real number.

## Solution:

4. Prove there is a unique function $f(x)$ such that $f^{\prime}(x)=2 x$ and $f(0)=3$. You may assume that if two functions have the same derivative then they differ by a constant. You may not integrate as part of your proof!

## Solution:

