## MATH310 Homework 2022-07-18 Due Gradescope 11:59pm 2022-07-20

1. Suppose $x$ is an integer. Prove by contrapositive that if $x^{2}$ is not divisible by 4 then $x$ is odd. [25 pts]
2. Suppose $x$ is a real number. Prove that if $x(x-4)>-3$ then $x<1$ or $x>3$.
3. Prove by contradiction that if $n$ is a natural number that:

$$
\frac{n}{n+1}<\frac{n+1}{n+2}
$$

4. Suppose $a$ and $b$ are positive integers. Prove by contradiction that if $a<b$ and $a b<3$ then [25 pts] $a=1$
