## MATH310 Homework 2022-07-27 Due Gradescope 11:59pm 2022-07-29

1. Use strong induction to prove that any postage greater than or equal to 18 cents can be made [ 40 pts ] from 3 and 10 cent stamps.
2. Define the recursive sequence:

$$
a_{1}=3, a_{2}=6 \text { and } a_{n}=5 a_{n-1}-6 a_{n-2}+2 \text { for } n \geq 3
$$

Use strong induction to prove that $a_{n}=1+2^{n-1}+3^{n-1}$ for all $n \in \mathbb{N}$.
3. Use weak induction to prove that for $n \geq 2$ that a $2^{n} \times 2^{n}$ chessboard with a corner piece [20 pts] missing can be covered completely by pieces shaped like:


