

## **MATH/CMSC 456, Jeffrey Adams**

Review for Final, May 18, 2009 (8-10 AM, Math B0429)

### 1. Chapter 2

- (a) Shift and affine ciphers
- (b) Vigenère cipher
- (c) Block ciphers, Hill cipher
- (d) One-time pads
- (e) Linear feedback shift registers

### 2. Chapter 3

- (a) Prime numbers
- (b) Euclidean algorithm, greatest common divisor, extended Euclidean algorithm
- (c) Chinese Remainder Theory
- (d) Congruences
- (e) Inverses  $(\text{mod } n)$ , solving  $ax = b \pmod{n}$
- (f) Fermat's and Euler's theorems

### 3. Chapter 4 The main thing to understand is the idea of Feistel systems. Also DES is not a group, triple DES, meet-in-the-middle attacks.

### 4. Chapter 6

- (a) Public Key Cryptography
- (b) Definition of RSA
- (c) Primality testing and factoring:
  - i. the Basic Principle (page 176)
  - ii. Fermat test
  - iii. p-1 factoring algorithm
  - iv. Miller Rabin and Universal Exponent method
  - v. Quadratic Sieve

### 5. Chapter 7

- (a) Basics of discrete logarithms
- (b) Pohlig-Hellman
- (c) Baby Step, Giant Step
- (d) Diffie Hellman key exchange
- (e) ElGamal cryptosystem

6. Chapter 8 (Hash Functions)
  - (a) Basics of hash functions
  - (b) Birthday attacks
  - (c) Birthday attack on discrete logarithms
7. Chapter 9 (Digital Signatures)
  - (a) Basic idea of digital signatures
  - (b) RSA signatures
  - (c) ElGamal signatures (you don't need to remember the formula)
  - (d) Hashing and signatures
  - (e) Birthday attacks on digital signatures
8. Chapter 12 (Secret Sharing)
  - (a) Basic concept of secret sharing
  - (b)  $(t, w)$ -threshold schemes
  - (c) Shamir threshold scheme
9. Chapter 14 (Zero Knowledge)
  - (a) Basic concept of zero-knowledge
  - (b) Square-root zero knowledge algorithm
10. Chapter 16 (Elliptic Curves)
  - (a) Basic concepts of elliptic curves
  - (b) Addition law on an elliptic curve
  - (c) Hasse's theorem
  - (d) Discrete logarithms on elliptic curves
  - (e) Representing plaintext
  - (f) Factoring with elliptic curves
  - (g) ElGamal on elliptic curves
  - (h) Diffie-Hellman on elliptic curves