

## HANDOUT

(1) Find the limit where required and use the definition of limit to prove each part.

(a)  $\lim_{n \rightarrow \infty} \frac{2n + 1}{3n - 1} = \frac{2}{3}$ .

(b)  $\lim_{n \rightarrow \infty} \frac{1}{1 + 3n} = 0$ .

(c)  $\lim_{n \rightarrow \infty} \frac{2n + 4}{5n + 2}$ .

(d)  $\langle a \rangle$  where  $a_n = 3 + 2^{-n}$ .

(2) If  $a_n^2$  converges as  $n \rightarrow \infty$ , does  $\lim_{n \rightarrow \infty} a_n$  need to exist? Give a proof or counterexample.