# Reducing Genome Assembly Complexity with Optical Maps 

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## Genome Assembly with de Bruijn Graphs

$$
\text { Genome = ACTACTGACT, K = } 4
$$




Equivalently:


- Multidigraph with one strongly connected component.
- Reconstruction of genome is an Eulerian tour
- In-degree = Out-degree
- Nodes labeled with sequence of length K-1
- Overlaps of K-2 bases
- \# of Eulerian tours combinatorial in the number of repeats


## Graph Simplification Operations

Spliting half decision nodes


Converting non-decision nodes to edges

Kingsford, C., Schatz, M. C., \& Pop, M. (2010). Assembly complexity of prokaryotic genomes using short reads. BMC bioinformatics, 11, 21.

## de Bruijn Graph <br> Mycoplasma genitalium ( $\mathrm{K}=100$ )



## Experimental Overview

## Optical Mapping



## Project Goals

- Develop the Contig-Optical Map Alignment Tool.
- Aligns contigs to an optical map based on restriction pattern with sequence information.
- Evaluate significance of alignments through a permutation test.
- Develop the Graph Simplification Tool, with functionality to:
- Read and write graphs to/from files.
- Count the number of unique shortest paths between two nodes.
- Modify the graph by replacing a selected path with a single edge.
- Simplify the graph through path compression.
- Develop a Pipeline:
- Integrate the Contig-Optical Map Alignment Tool and Graph Simplification Tool.
- Generates simulated optical maps.
- Evaluate the correctness of the graph simplification operations
- Write debug level logs files and summary files to disk.
- Submit jobs to Condor cluster.
- Validate pipeline on dataset of 351 prokaryotic reference genomes.


## Project Schedule \& Milestones

## Phase I (Sept 5 - Nov 27)

- Complete code for the contig-optical map alignment tool (C++)
- Test algorithm by aligning user-generated contigs to user-generated optical map
- Begin implementation of networkx for working with assembly graphs


## Phase II (Nov 27 - Feb 14)

- Finish de Bruijn graph utility functions.
- Complete code for the assembly graph simplification tool (Python)
- Test assembly graph simplification tool on simple user-generated graph.
- Implement parallel implementation of the contig-optical map alignment tool using OpenMP


## Phase III (Feb 14 - May 8)

- Integrate alignment tool and graph simplification tool into a single pipeline (Python)
- Validate performance of the contig-optical map alignment tool and the graph simplification tool with archive of de Bruijn graphs for reference bacterial genomes.
- Compute reduction in graph complexities.


## Algorithmic Recipe

1. Align contigs (graph edges) to optical map
2. Tile uniquely aligned contigs across optical map
3. Find shortest paths between aligned contig
 neighbors.
4. Select unique shortest paths as gap closure candidates.
5. Perform global alignment of gap closure candidate to the optical map and accept/reject path.
6. Replace accepted paths in the graph with a single edge.
7. Perform path compression.
8. Evaluate graph correctness


## Contig-Optical Map Alignment Tool

## Scoring Alignments

- $o_{i}$ : Optical restriction fragment mean length
- $\sigma_{i}$ : Optical restriction fragment standard deviation
- $c_{i}$ : contig restriction fragment length
$\chi^{2}$ scoring function for alignment of contig at position $j$ of optical map:

$$
S_{\chi^{2}}=\sum_{i=1}^{n}\left(\frac{c_{i}-o_{i+j}}{\sigma_{i+j}}\right)^{2}
$$



## Scoring Alignments

- $d_{i}$ : edit distance at $i$ th aligned restriction site
- $m_{r}$ : number of missed restriction sites of alignment
- $C_{r}, C_{s}$ : constant weights

Alignment score:

$$
S=S_{\chi^{2}}+C_{r} \times m_{r}+C_{s} \times \sum_{i=1}^{n-1} d_{i}
$$

The best match is given by the lowest score.


## Alignment Algorithm



- $S_{i j}$ : Score of the best alignment of contig through $i$ th fragment with optical map through $j$ th fragment.
- Find $S_{i j}$ by extending a previously scored alignment $S_{i^{\prime}, j^{\prime}}$ where $0 \leq i^{\prime}<i, 0 \leq j^{\prime}<j$.
$S_{i j}=\min _{0 \leq k \leq i, 0 \leq l \leq j} C_{r} \times(i-k+j-l)+C_{s} \times d_{i j}+\frac{\left(\sum_{s=k}^{i} c_{s}-\sum_{t=l}^{j} o_{t}\right)^{2}}{\sum_{t=l}^{j} \sigma_{t}^{2}}+S_{(k-1)(l-1)}$
Missed restriction sites
Sequence Edit Distance
Prefix alignment score

Assembly Graph Simplification Tool

## Count Number of Shortest Paths

- Goal: Count the number of unique shortest paths from source node to target node.
- Dijkstra's algorithm: O(E + V log(V))
- Store examined nodes with tentative distances in a priority queue.
- Store set of visited nodes.
- For each node store a set of predecessors on shortest paths from source.


| Distance from A: | Predecessors |
| :--- | :--- |
| A: 0 | A: [ ] |
| B: 2 |  |
| D: 1 | B: [A] |
| C: 3 | D: [A] |
| E:2 | C: [B,D] |
|  | E: [D] |

Node Paths: [A,B,C], [A,D,C]
Edge Paths: [(A,B,0), (B,C,O)]

$$
\begin{aligned}
& {[(\mathrm{A}, \mathrm{~B}, 0),(\mathrm{B}, \mathrm{C}, 1)]} \\
& {[(\mathrm{A}, \mathrm{~B}, \mathrm{1}),(\mathrm{B}, \mathrm{C}, 0)]} \\
& {[(\mathrm{A}, \mathrm{~B}, \mathrm{1}),(\mathrm{B}, \mathrm{C}, 1)]} \\
& {[(\mathrm{A}, \mathrm{D}, \mathrm{O}),(\mathrm{D}, \mathrm{C}, 0)]}
\end{aligned}
$$

Edge denoted by (Node 1, Node 2, Edge Key)

## Graph Simplification

- Replace a given path with a single edge.
- Delete any disconnected nodes.
- Perform path compression. (A $\rightarrow \mathrm{C} \rightarrow \mathrm{H}$ )
- Assert validity of the graph



## Validate on 351 Prokaryotic Genomes

- Simulate optical maps from reference genomes.
- Enzyme $=$ BamHI (GGATCC), K=100, Fragment Variance $=0.3$ * Fragment Length
- No error
- Low error (sizing error s.d = 1\%, 10\% substitutions, $5 \%$ missing sites)
- High error (sizing error s.d. $=5 \%, 20 \%$ substitutions, $10 \%$ missing sites)
- Evaluate alignment correctness:
- Alignment within $0.1 \%$ of true contig location
- Evaluate path correctness for selected closure paths using longest common subsequence.
- True path: [(A,B,0), (B,C,1), (C,F,0), (F,D,2)]
- Selected Path: [(A,B,0), (B,C,1),(C,E,1),(E,F,0),(F,D,2)]
- Common path length from edges (A,B,0) + (F,D,2)
- Path correctness is ratio of common length to true length

[(B,C), (C,F)]
- Evaluate reduction in complexity. Example: a = 3


$$
\begin{aligned}
& C(v)=\sum_{i=2}^{a} i=\frac{a(a+1)}{2}-1 \\
& C(G)=\sum_{v \in V} C(v)
\end{aligned}
$$

## Validation Data Set: 351 Genomes

## Contig Count Distribution

## Genome Size Distribution




## Validation Data Set: 351 Genomes



Complexity vs. Genome Size


## Alignment Results: <br> (Error Free Optical Map)

Number of Contigs Aligned


## Number of Contigs Aligned



- All aligned contigs have an alignment in correct position (within $0.1 \%$ of true location)


## Alignment Results: (Error Free Optical Map)

## Unaligned Contig Counts

Outlier: Nocardia farcinica (NC_006361)

- Many contigs with "uninformative" restriction pattern
edge_40_88_0 3110.0
/cbcb/project-scratch/lmendelo/debruijn/condor/no
Contig Frags | Optical Frags
$\begin{array}{rl}220=220 & \mathrm{G} ; \mathrm{G} \\ 12=12 \quad \mathrm{C} ; \mathrm{G} & 1246=12 \mathrm{C}=12 \mathrm{C} ; \mathrm{G} \\ 79=79 & \\ 0.0 \\ \text { ratch/lmendelo/debruijn/condor/no }\end{array}$
Contig Frags I Optical Frags
$220=220 \mathrm{G} ; \mathrm{G} \mid 1431=1431 \mathrm{G} ; \mathrm{G}$ $12=12 \quad C ; G \mid 12=12 \quad C ; G$ $79=79$
$1223=122$
edge_40_88_0 311 0.0
/cbcb/project-scratch/lmendelo/debruijn/condor/no
Contig Frags | Optical Frags
$220=220 \mathrm{G} ; \mathrm{G} \mid 5221=5221 \mathrm{G} ; \mathrm{G}$ $12=12 \quad C ; G \mid 12=12 \quad C ; G$ $79=79 \quad \mid 2664=2664$
- 


edge_40_88_0 311 0.0
/cbcb/project-scratch/lmendelo/debruijn/condor/no
Contig Frags | Optical Frags

| 220 | $=220$ | $\mathrm{G} ; \mathrm{G}$ | $702=702 \mathrm{G} ; \mathrm{G}$ |
| ---: | :--- | :--- | :--- |
| $12=12$ | $\mathrm{C} ; \mathrm{G}$ | $12=12 \mathrm{C} ; \mathrm{G}$ |  | $\begin{aligned} & 12=12 \\ & 79=79\end{aligned} \quad C ; G \left\lvert\, \begin{aligned} & 12=12 \quad C \\ & 3076=3076\end{aligned}\right.$

## Number of Shortest Paths (Error Free Optical Map)

Distribution of Number of Path Closures
Distribution of Log10(Number of Closures)



## Accepted Path Closures (Error Free Optical Map)

Distribution of Normalized Closure Path Lengths


Sequence Difference for selected and true paths


## Improvements To Assembly (Error Free Optical Map)

Fold Change in N50


Reduction in Complexity


## NC_000868 Pyrococcus abyssi

 (Error Free Optical Map)Original Graph


Final Graph



NC_005823

## Pyrococcus abyssi

## Genome size: <br> 4.3 Mbp

Nodes: 134
Edges: 415
N50: 55,117
Complexity: 1007


NC_005823

## Pyrococcus abyssi

Genome size:
4.3 Mbp

Nodes: 104
Edges: 309
N50: 124,312
Complexity: 707
Incorrect: 2,373 out of
2,722,585

## Results Across Error Settings

Number of Contigs Aligned Uniquely


Reduction in Complexity


## Run Times

## CBCB Condor Cluster:

24 nodes
12 cores, 48 GB RAM

Mean run time $\sim 4$ minutes Median run time $\sim 1$ minute

## Conclusions \& Potential Improvements

## Conclusions

- Unique shortest path heuristic works well (when a unique shortest path exists).
- Many contigs are "unalignable" due to lack of restriction sites or uninformative restriction patterns.
- Most of the repeat structure of the genome is contained in a small fraction of the genome.

Potential Improvements

- Choose the most informative restriction enzyme for the genome.
- Use multiple rounds of contig alignment and graph simplification.
- Combine paired read information with optical maps.
- Use multiple optical maps.


## Deliverables

- Source code for contig-optical map alignment tool
- Source code for graph simplification tool
- Source code for pipeline
- Log files \& summary files for simulations
- Written report


## References

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## Alignment Algorithm

$$
\begin{array}{lll}
S_{00} & S_{01} & S_{2} \\
S_{10} & S_{11} & S_{12}
\end{array}
$$


$S_{11}\left(\right.$ uses $\left.S_{00}\right)$


- $S_{i j}$ : Score of the best alignment of contig through $i$ th fragment with optical map through $j$ th fragment.

