

University of Baltimore  
 Math 321: Discrete Structures  
 Worksheet for Chapter 3: Function exercises

1. Given the function  $f(n) = 2n + 1$ , evaluate  $f(0)$ ,  $f(1)$ ,  $f(2)$  and  $f(3)$ .
2. Given the function  $f(n) = n^2 - n$ , evaluate  $f(0)$ ,  $f(1)$ ,  $f(2)$  and  $f(3)$ .
3. Given the function  $f(n) = \frac{n+3}{n!}$ , evaluate  $f(0)$ ,  $f(1)$ ,  $f(2)$  and  $f(3)$ .
4. Given the function  $f(n) = \begin{cases} n+1, & n \leq 2 \\ n-1, & n > 2 \end{cases}$ , evaluate  $f(0)$ ,  $f(1)$ ,  $f(2)$  and  $f(3)$ .
5. Given the function  $f(n) = \begin{cases} f(0) = 0 \\ f(n) = n^2 - 1, & n \geq 1 \end{cases}$ , evaluate  $f(0)$ ,  $f(1)$ ,  $f(2)$  and  $f(3)$ .
6. Given the function  $f(n) = \begin{cases} f(0) = 0 \\ f(n) = [f(n-1)]!, & n > 0 \end{cases}$ , evaluate  $f(0)$ ,  $f(1)$ ,  $f(2)$  and  $f(3)$ .
7. Given the function  $f(n) = \begin{cases} f(0) = 1 \\ f(n+1) = f(n) + 2, & n \geq 0 \end{cases}$ , evaluate  $f(0)$ ,  $f(1)$ ,  $f(2)$ ,  $f(3)$  &  $f(4)$ .
8. Given  $f(n) = \begin{cases} f(0) = 1 \\ f(1) = 3 \\ f(n+2) = 2f(n+1) - f(n), & n \geq 0 \end{cases}$ , evaluate  $f(0)$ ,  $f(1)$ ,  $f(2)$ ,  $f(3)$  &  $f(4)$ .
9. Of the functions given above, which ones are recursive functions?

Answers: 1) 1, 3, 5, 7      2) 0, 0, 2, 6      3) 3, 4,  $\frac{5}{2}$ , 1      4) 1, 0, 3, 2  
 5) 0, 0, 3, 8      6) 0, 1, 1, 1      7) 1, 3, 5, 7, 9      8) 1, 3, 5, 7, 9