

MATH 141, FALL 2011

Investigate the convergence of the following positive series:

$$\sum_{n=1}^{\infty} \frac{1}{\sqrt{n(n+1)}} \quad \text{divergent}$$

$$\sum_{n=1}^{\infty} \frac{1000^n}{n!} \quad \text{convergent}$$

$$\sum_{n=1}^{\infty} \frac{(n!)^2}{(2n)!} \quad \text{convergent}$$

$$\sum_{n=1}^{\infty} \frac{n!}{n^n} \quad \text{convergent}$$

$$\sum_{n=1}^{\infty} \frac{2^n n!}{n^n} \quad \text{convergent}$$

$$\sum_{n=2}^{\infty} \frac{1}{\sqrt[n]{\ln(n)}} \quad \text{divergent}$$

$$\sum_{n=1}^{\infty} \frac{n^5}{2^n + 3^n} \quad \text{convergent}$$

$$\sum_{n=1}^{\infty} \frac{3 + (-1)^n}{2^{n+1}} \quad \text{convergent}$$

$$\sum_{n=2}^{\infty} \frac{1}{n \ln^p(n)} \quad \text{convergent for } p > 1$$

$$\sum_{n=2}^{\infty} \frac{1}{n \ln^p(n) \ln^q(\ln(n))} \quad \text{convergent for } p > 1 \text{ and any } q, \text{ or for } p = 1 \text{ and } q > 1$$