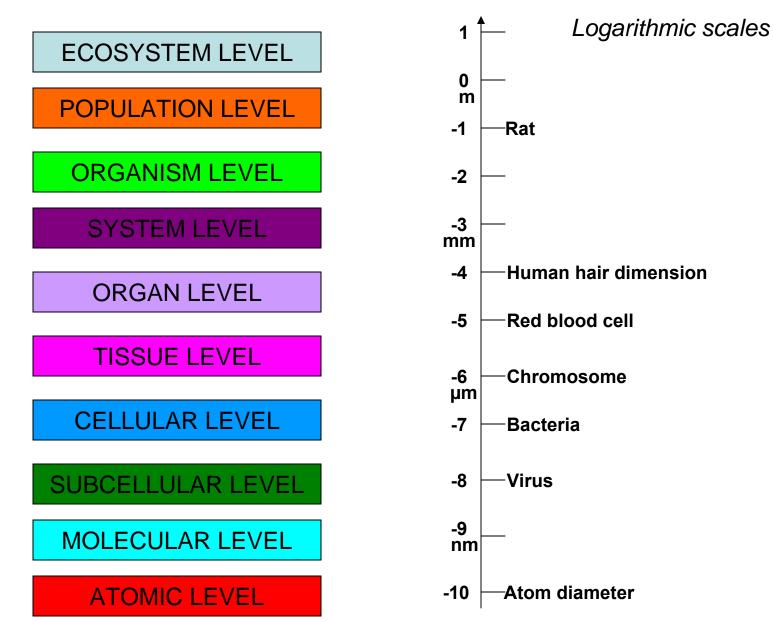
# Multiscale Approach to Protein Engineering in Bioluminescence Probe Design

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"Kinetic Description of Multiscale Phenomena" Workshop CSCAMM, University of Maryland March 2-5, 2009

# **Multiscale in Biology**



# Mathematics Data analysis Biology Challenge to deal with heterogeneity

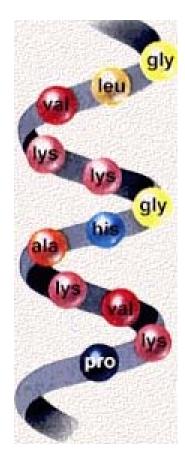
### Mathematics Is Biology's Next Microscope, Only Better;

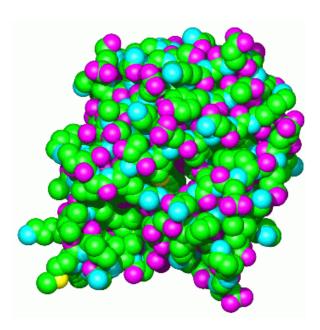
### Biology Is Mathematics' Next Physics, Only Better

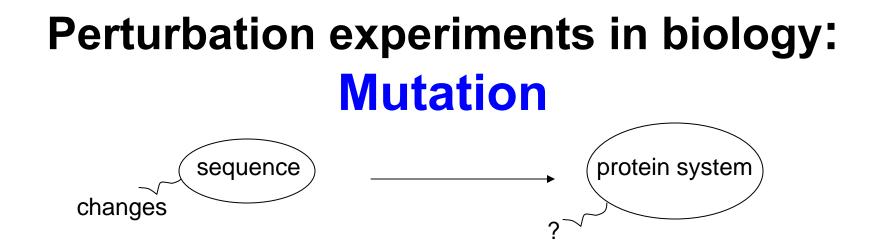
# **Protein Structure**



Primary structure
Secondary structure
Tertiary structure







#### **Responses to mutation:**

- no responses or localized responses
- cascading effects

# **Protein Engineering**

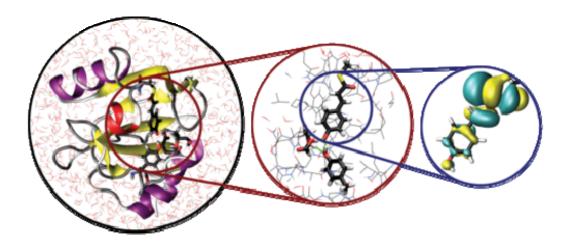
**Goal:** find the sequence -> desired properties

**Idea:** alter the sequence -> alter the properties

Methods: • rational design

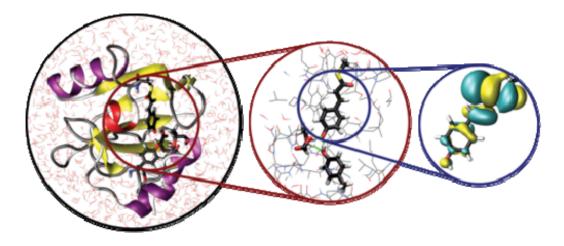
directed evolution

### **Multiscale Modeling for Proteins**



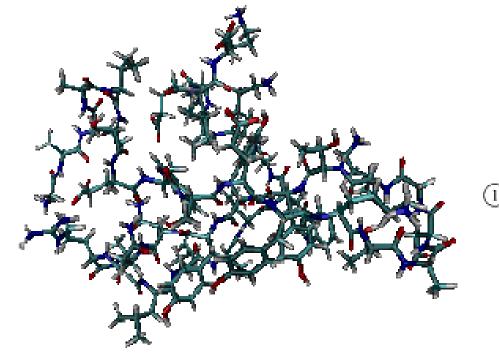
### **Multiscale Modeling for Proteins**

#### "zoom-in" does NOT work!



### **Multiscale Modeling for Proteins**

- A whole-system study at all scales
- Multiscale: different resolutions

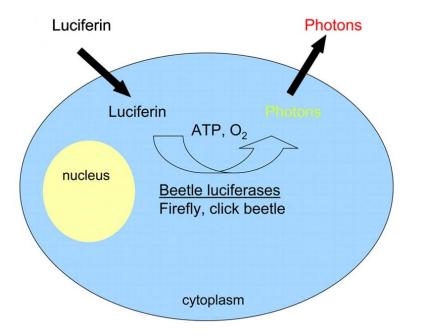


network model (simplified potential)

atomistic model (QM/MM)

### **Bioluminescence**

#### conversion of chemical energy into light

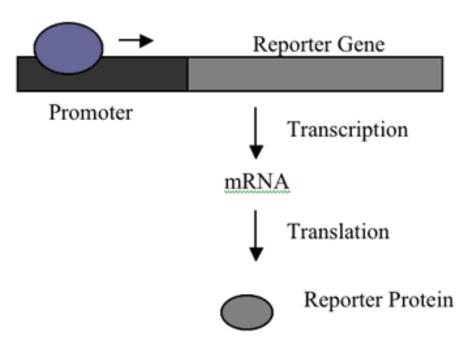




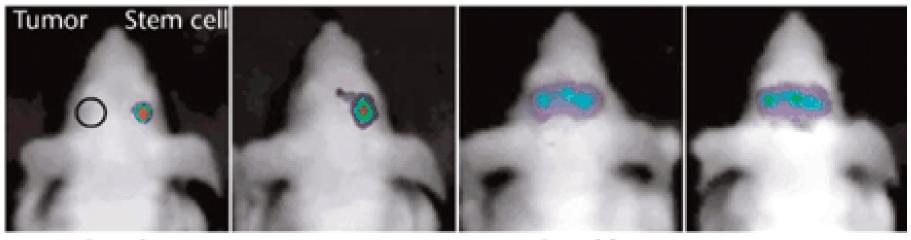
# Bioluminescence Reporter Gene Imaging

Insert the reporter gene to the gene of interest

to create a gene fusion.



### **Example of Bioluminescence Imaging**



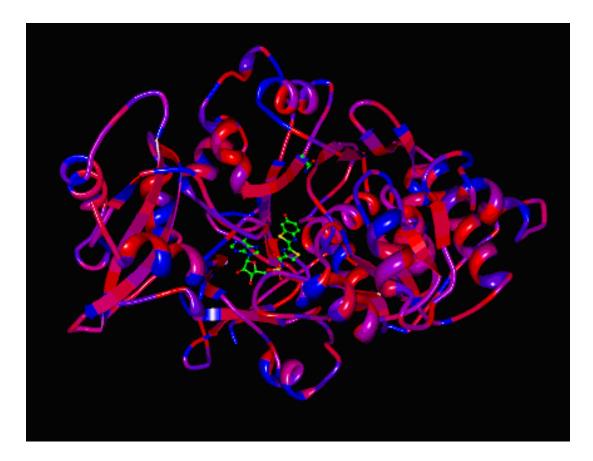
Day 9Day 15Day 22Day 36Migration of neural progenitor stem cells (labeled with the luciferin)<br/>across the midline towards an implanted brain cancer in a mouse.

A Dzik-Jurasz, British Journal of Radiology (2003) 76, S98-S109

# Challenge:

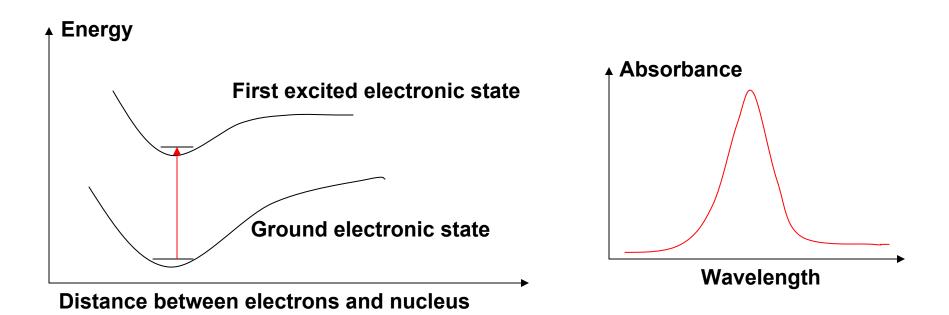
#### How to achieve Red Emission of Bioluminescence?

# Luciferase•DLSA complex

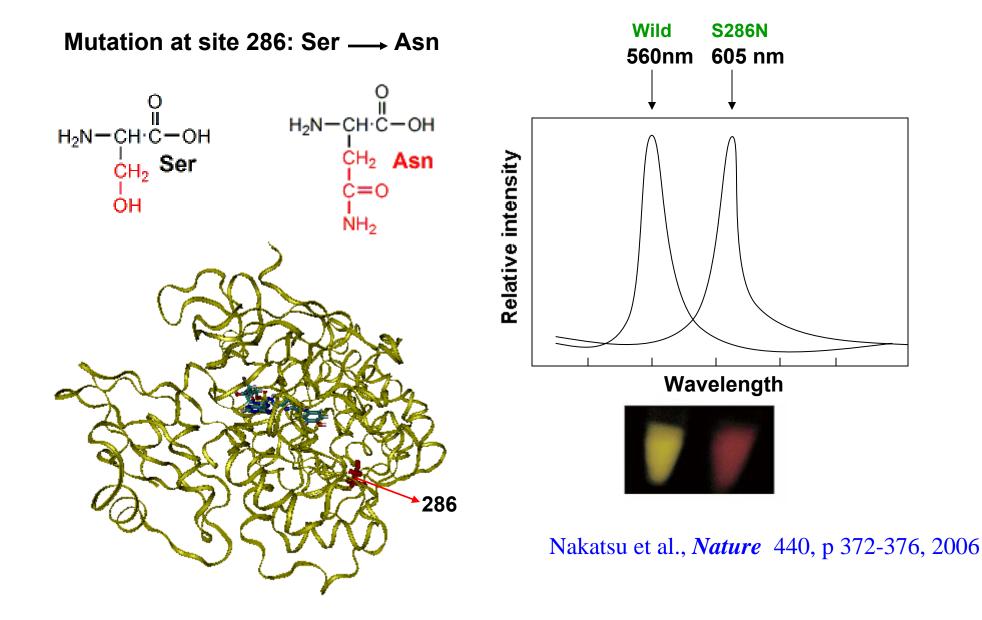


Luciferase (protein): catalyst, 539 residues, 8451 atoms DLSA: light emitter, 58 atoms

#### **Excitation of DLSA**



#### Luciferase: Spectral Shift

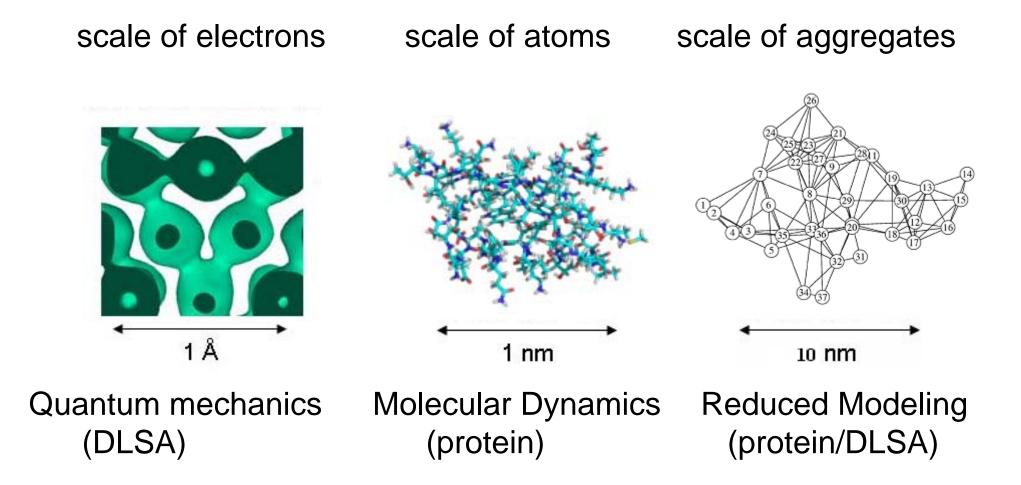


# Goal

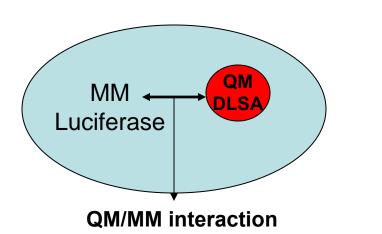
• At the **atomic** level, explain the physical origin of the spectral shift caused by mutation.

• At the sequence level, design the system (luciferase) with desired optical property.

# The matter of scale



# Hybrid Quantum Mechanical/Molecular Mechanical (QM/MM) Approach



QM:  $\hat{H}\psi = E\psi$ MM: F =  $-\partial \hat{H}/\partial q$ 

Hamiltonian:  $\hat{H}_{total} = \hat{H}_{QM} + \hat{H}_{MM} + \hat{H}_{QM/MM}$  $\hat{\mathbf{H}}_{\mathbf{QM}} = -\frac{1}{2} \sum_{i} \nabla_{i}^{2} + \sum_{ii} \frac{1}{r_{ii}} - \sum_{i\alpha} \frac{Z_{\alpha}}{r_{i\alpha}} + \sum_{\alpha\beta} \frac{Z_{\alpha}Z_{\beta}}{r_{\alpha\beta}}$  $\hat{\mathbf{H}}_{\mathbf{QM/MM}} = -\sum_{iM} \frac{q_M}{r_{iM}} + \sum_{\alpha M} \frac{Z_{\alpha} q_M}{R_{\alpha M}} + \sum_{\alpha M} \left(\frac{A_{\alpha M}}{R_{\alpha M}^{12}} - \frac{B_{\alpha M}}{R_{\alpha M}^{6}}\right)$  $\hat{\mathbf{H}}_{\mathbf{MM}} = \sum_{bonds} k_r (r - r_0)^2 + \sum_{angles} k_{\theta} (\theta - \theta_0)^2$ +  $\sum k_{\phi} [1 + \cos(n\phi + \phi_0)] +$ dihedrals  $\sum \left[ \sum \left\{ 4\varepsilon_{MN} \left[ \left( \frac{\sigma_{MN}}{2} \right)^{12} - \left( \frac{\sigma_{MN}}{2} \right)^{6} \right] + \frac{q_M q_N}{2} \right] \right\}$  $r_{MN}$  $r_{MN}$   $4\pi\varepsilon_0 r_{MN}$ atom  $M \neq N$ 

α,β: QM nuclei *i,j*: QM electron *M,N*: MM atoms

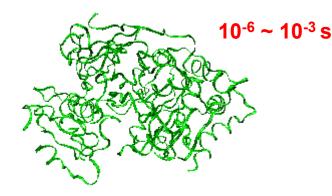
### **QM/MM Procedure**

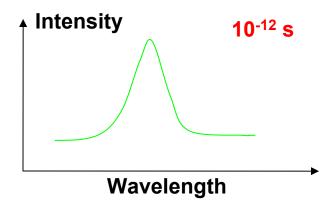
#### performed by ONIOM program (Gaussian 03)

• Start with the crystal structures

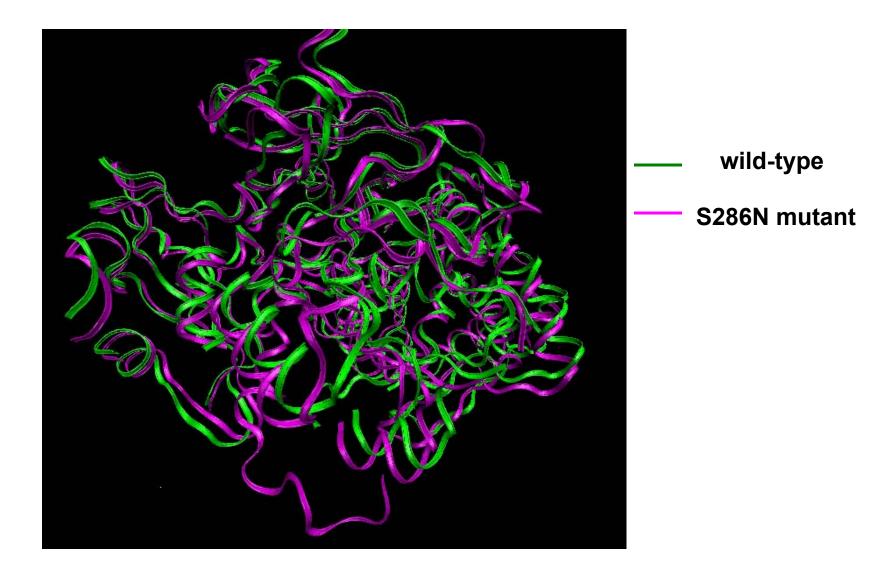
- The ground state is optimized at the ONIOM-EE (B3LYP/6-31G\*:AMBER) level
- The  $S_0 \rightarrow S_1$  excitation energy is computed by TDDFT/B3LYP/6-31G\*:AMBER based on the optimized ground state structure

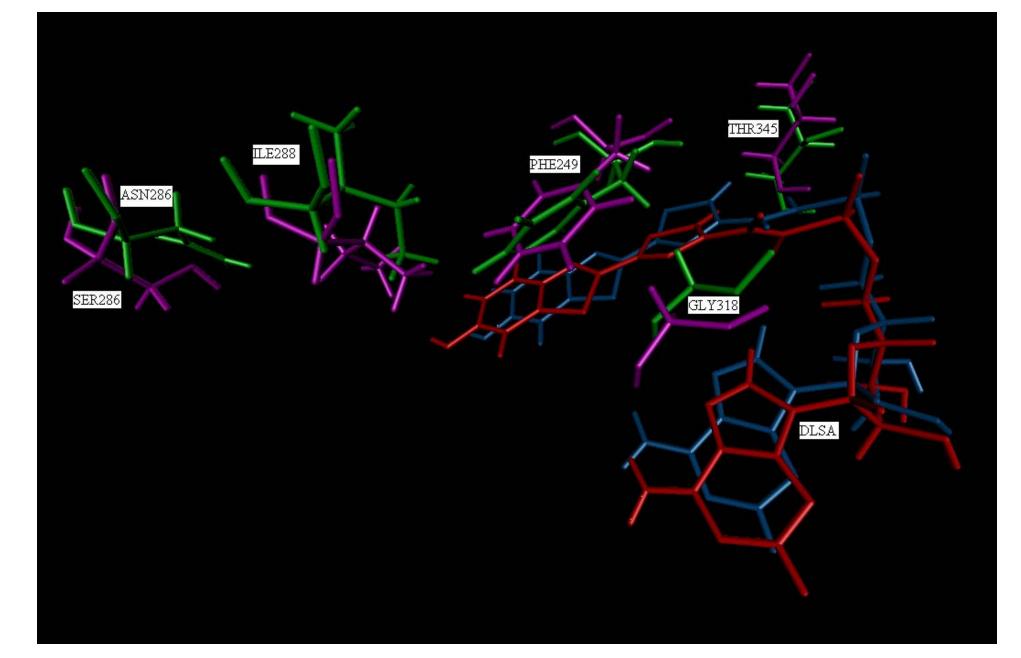
#### Assumption: time for structural relaxation >> time for electron excitation

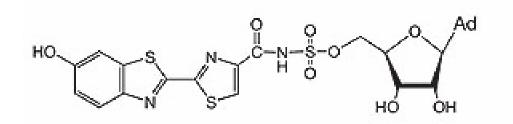




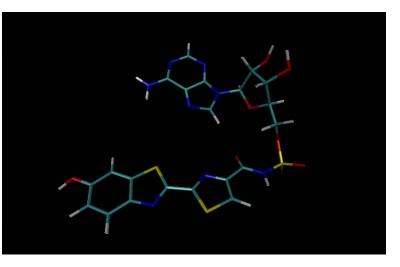
#### Global Structural Change Caused by Mutation S286N



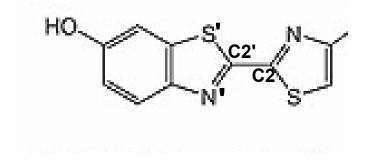




5'-O-[N-(dehydroluciferyl)-sulfamoyl]adenosine (DLSA)



	C2'-C2	C2'-N'	C2-S'	C2-N	C2-S	S'-C2'-C2-S	N'-C2'-C2-N
WT	1.4486Å	1.3073Å	1.7614Å	1.3074Å	1.7649Å	159.47°	163.60°
S286N	1.4483Å	1.3101Å	1.7604Å	1.3098Å	1.7661Å	172.39°	174.00°



# Luciferase Multicolor Bioluminescence Mechanism

- The effect of the protein environment is on the relative angle of two rings of DLSA through van der Waals contacts.
- A more planar two rings of DLSA leads a spectral redshift.

#### **The Calculated Emission Spectra**

	Calculated	Experimental Data	
Wild-type luciferase	589 nm	560 nm	
Mutant (S286N) luciferase	611 nm	605 nm	