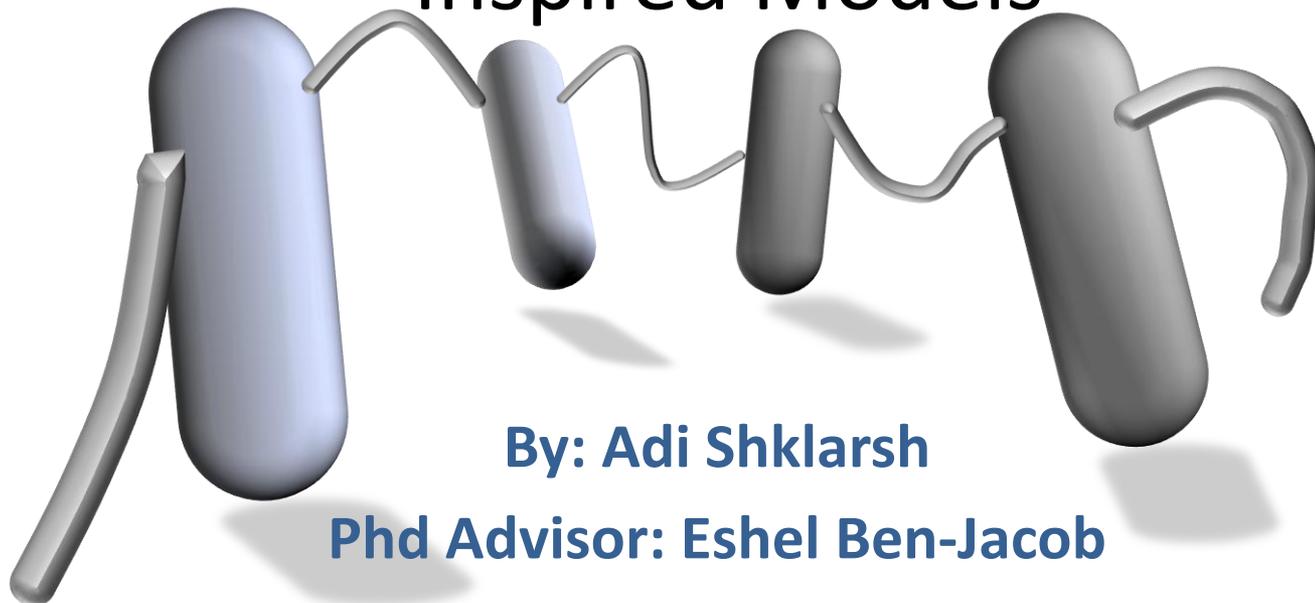


**Ki-net – 17.01.13**

# Complex Collective Navigation in Bacteria- Inspired Models

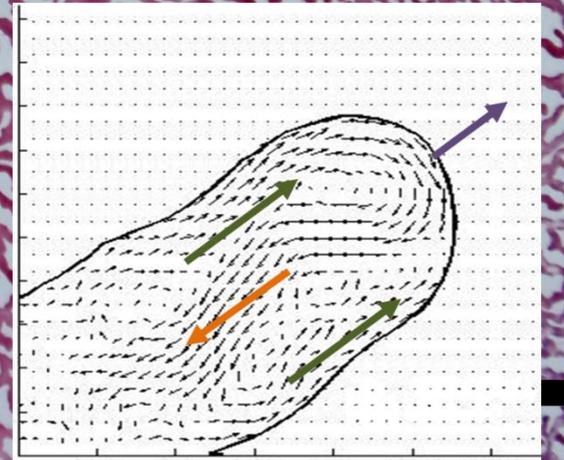
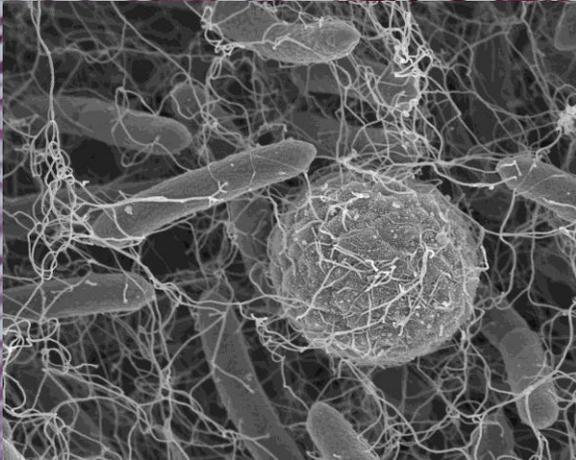
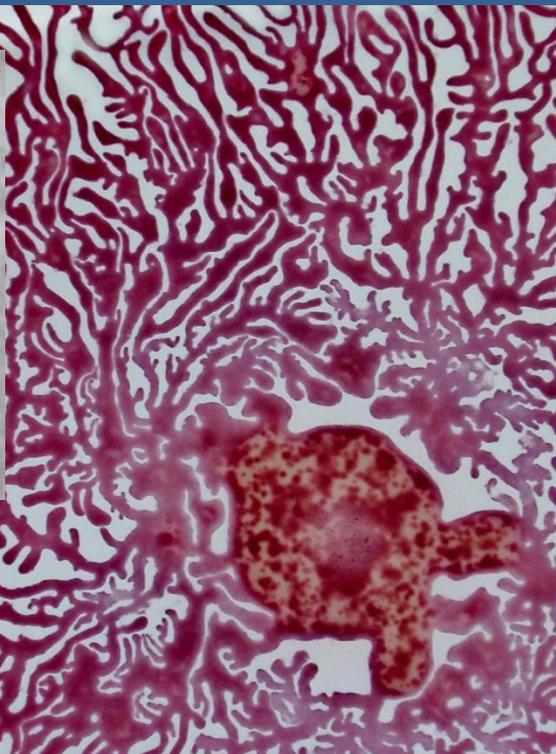
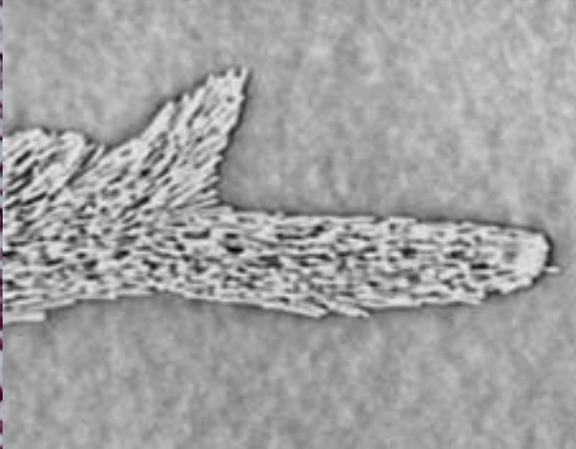


**By: Adi Shklarsh**

**Phd Advisor: Eshel Ben-Jacob**

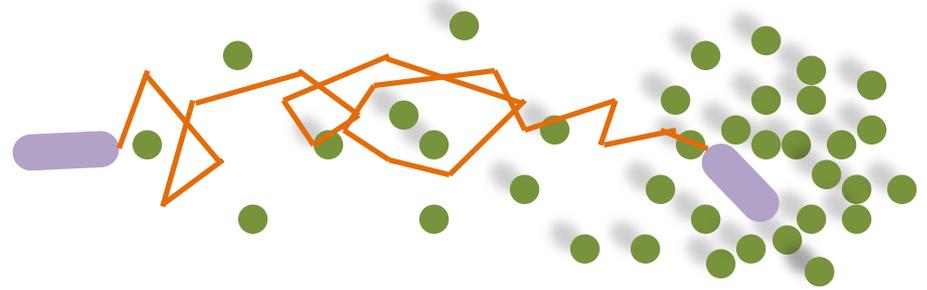
**Collaborators: Gil Ariel, Colin Ingham, Alin Finkelshtein**

# Bacteria collective behavior



# Bacteria tools

- Chemotaxis

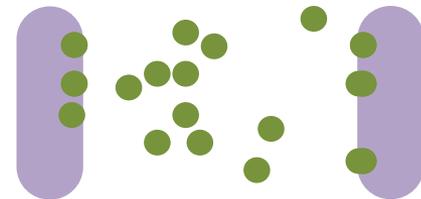


- Physical interactions



- Communication

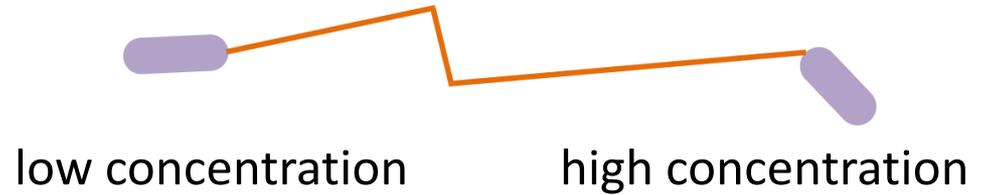
[Miller and Bassler 2001, Annual Reviews Microbiology ]



# Modeling Swarms

- Chemotaxis:

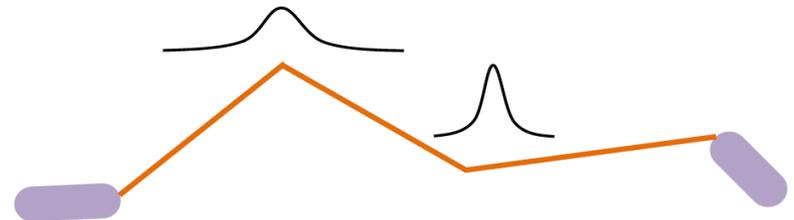
run and tumble



run time is a function of the temporal gradient

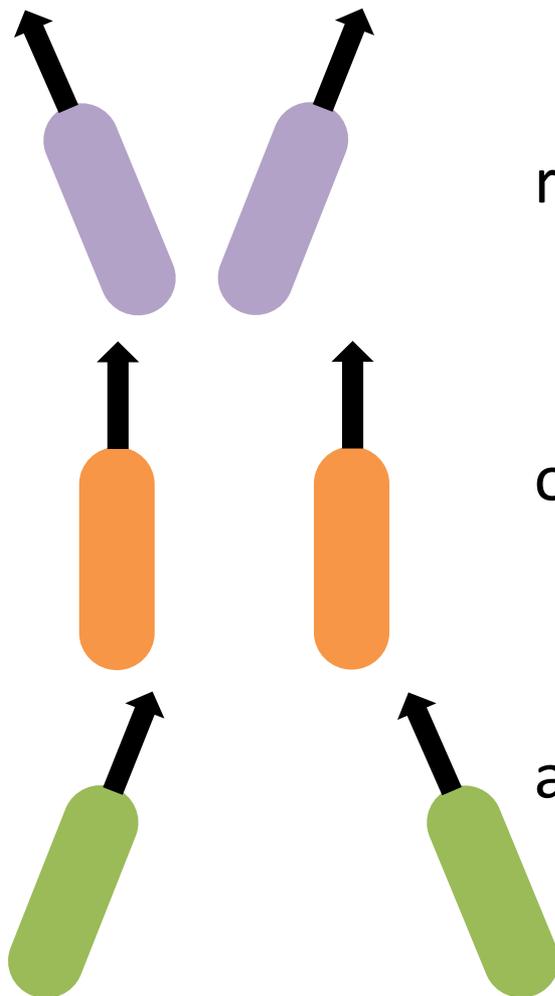
Model:

The angle depends on the temporal gradient



# Modeling Swarms

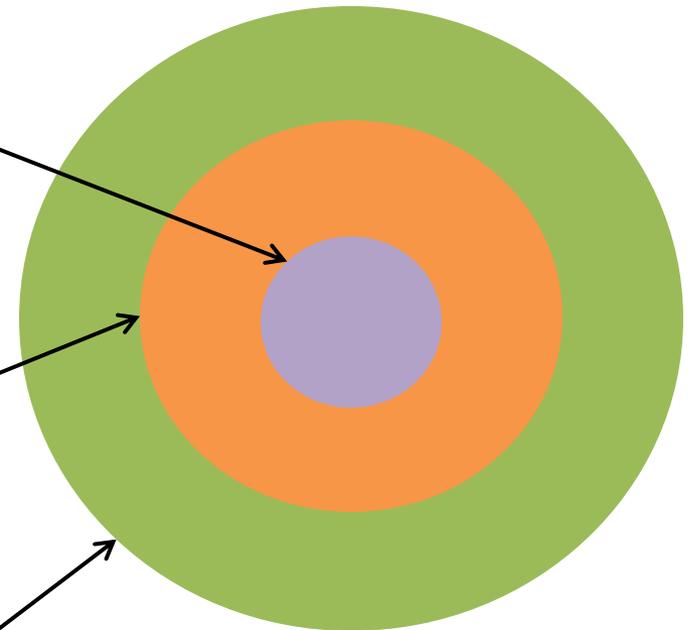
## Simple interactions



repulsion

orientation

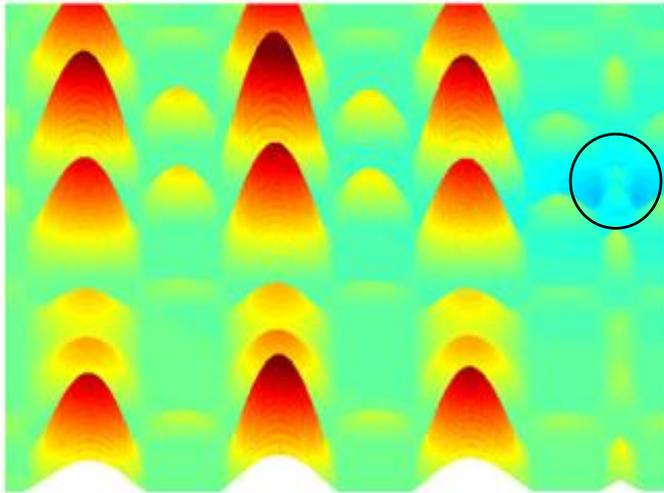
attraction



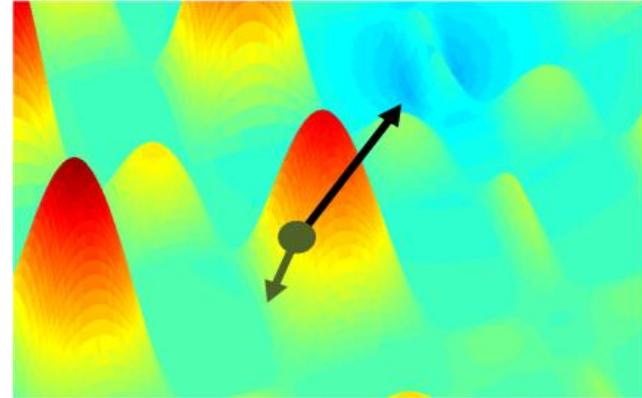
[Vicsek *et al.* 1995, Grunbaum 1998, Couzin *et al.* 2005]

# Navigation in complex terrain

The environment is constant in time and spatially noisy



$$\cos(\omega_1 x + \varphi_1) \cdot \cos(\omega_2 x + \varphi_2)$$



# Bacteria-Inspired Models

- **Adaptable Interactions**

[Shklarsh et al. 2011, Plos Computational Biology]

Elad Schneidman, Gil Ariel, Eshel Ben-Jacob

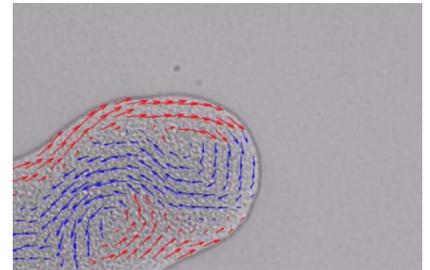
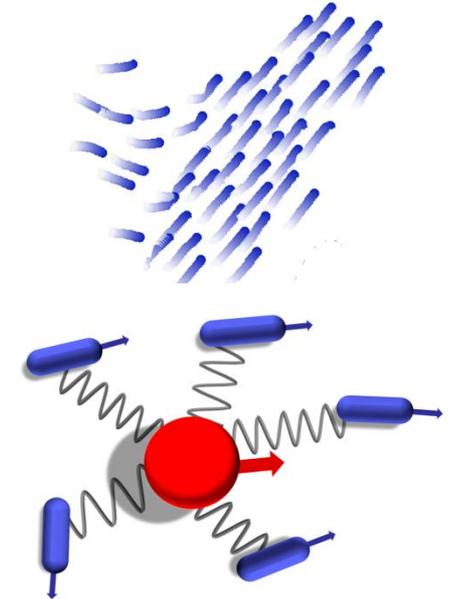
- **Cargo Carrying Swarms**

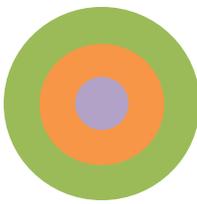
[Shklarsh et al. 2012, Interface Focus]

Alin Finkelshtein, Gil Ariel, Oren Kalisman, Colin Ingham, Eshel Ben-Jacob

- **Collective Dynamics**

Gil Ariel, Adi Shklarsh, Oren Kalisman, Colin Ingham, Eshel Ben-Jacob





# Modeling Bacteria Swarms

positions:  $\vec{r}_i(t)$   
velocity directions:  $\vec{v}_i(t)$ ,  $|\vec{v}_i(t)|=1$

run

$$\vec{v}_i(t+\Delta t) = \vec{d}_i(t) + w \cdot \vec{v}_i(t)$$

velocity direction

group influence

weight

previous velocity direction

$$\vec{d}_i(t) = - \sum_{j \in RR_i(t)} \frac{\vec{r}_j(t) - \vec{r}_i(t)}{|\vec{r}_j(t) - \vec{r}_i(t)|}$$

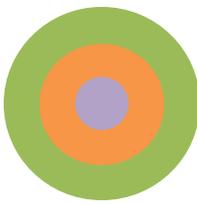
repulsion

or

$$\vec{d}_i(t) = \sum_{j \in RO_i(t)} \vec{v}_j(t) + \sum_{j \in RA_i(t)} \frac{\vec{r}_j(t) - \vec{r}_i(t)}{|\vec{r}_j(t) - \vec{r}_i(t)|}$$

orientation

attraction



# Modeling Bacteria Swarms

positions:  $\vec{r}_i(t)$   
velocity directions:  $\vec{v}_i(t)$ ,  $|\vec{v}_i(t)|=1$   
chemical concentration:  $c(x)$

**run**

$$\vec{v}_i(t+\Delta t) = \vec{d}_i(t) + w \cdot \vec{v}_i(t)$$

velocity direction

group influence

weight

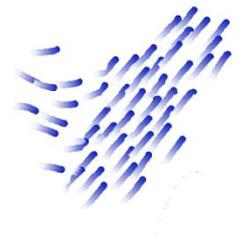
previous velocity direction

**tumble**

$$\text{gaussian noise}(c(\vec{r}(t)) - c(\vec{r}(t - \tau)))$$

constant measurement interval

# Adaptable interactions

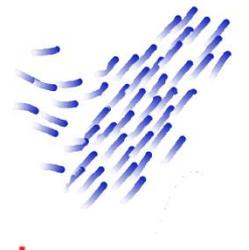


$$\vec{v}_i(t+\Delta t) = \vec{d}_i(t) + w_i(t) \cdot \vec{v}_i(t)$$

adaptable weights

$$w_i(t) = \begin{cases} 1 & \text{sign}(\text{grad}_i) > 0 \\ 0 & \text{else} \end{cases}$$

We consider adaptable interactions as a biologically-inspired design principle that will dynamically modify the behavior of the system in response to changes in the environment.

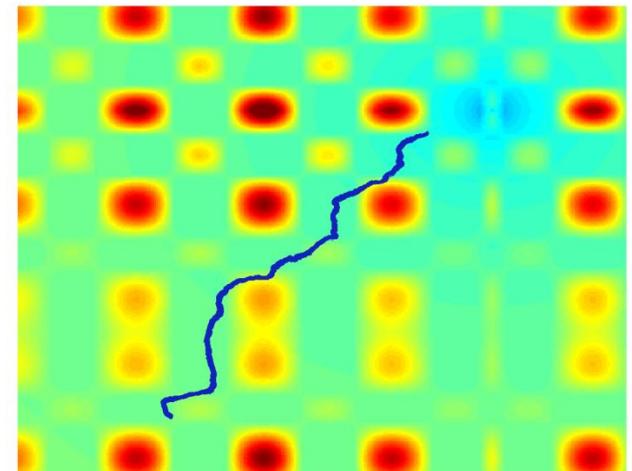
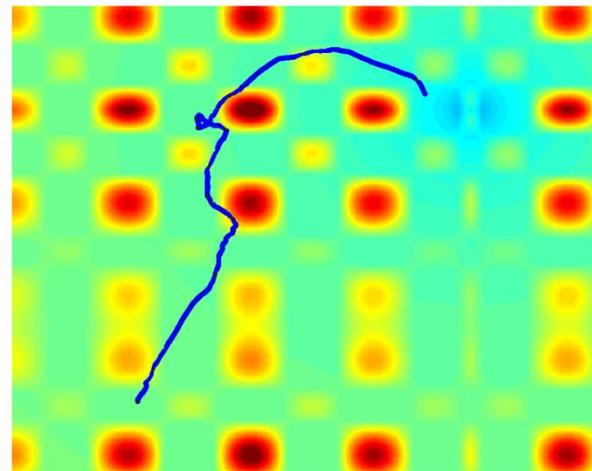
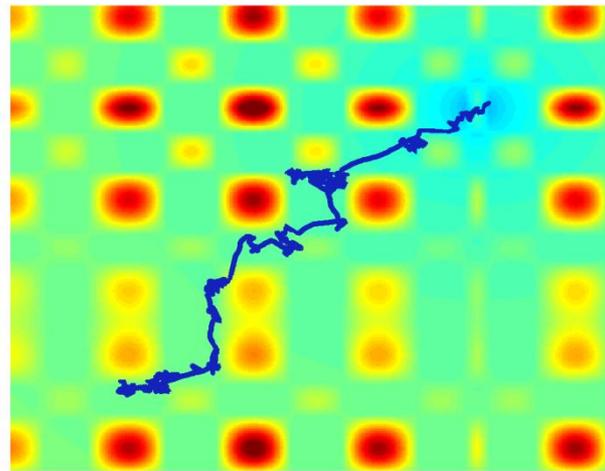
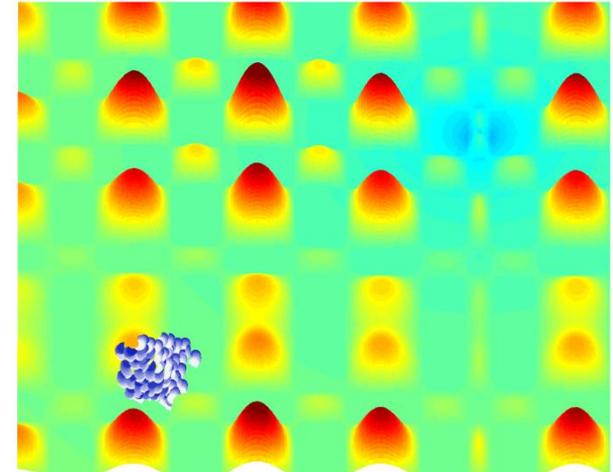
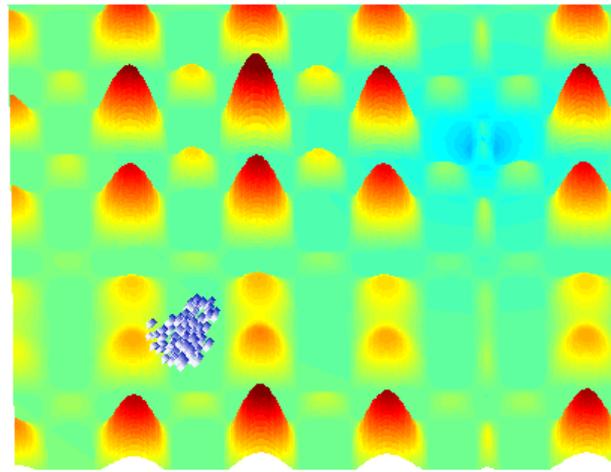
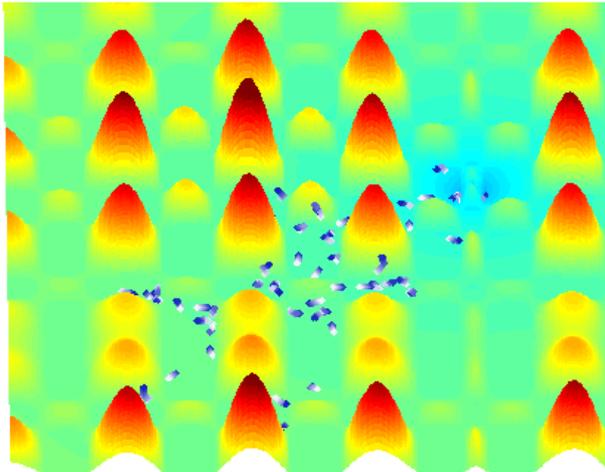


# Simulations

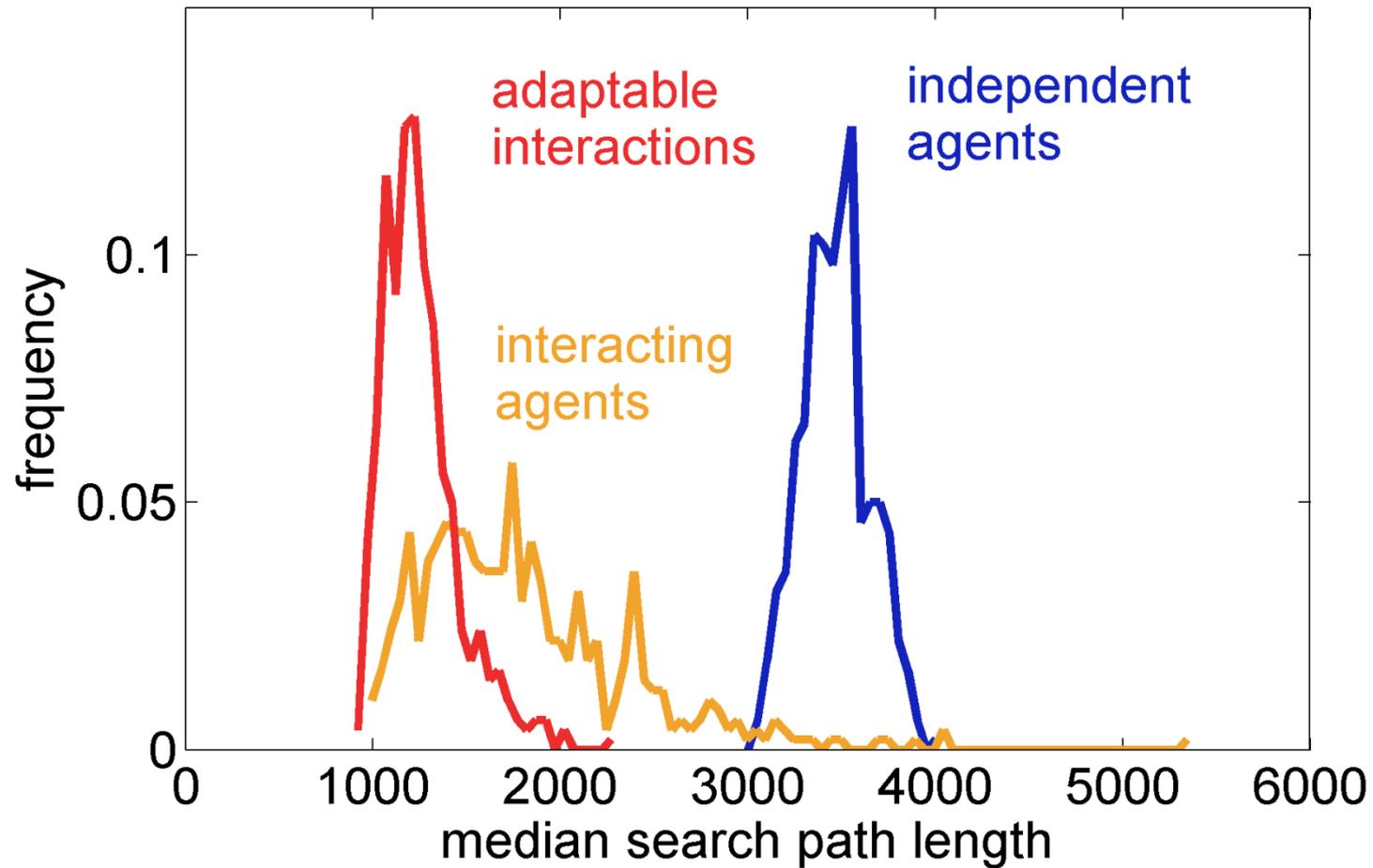
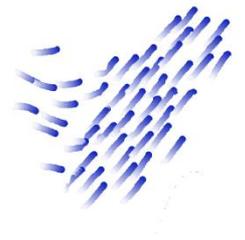
independent  
agents

interacting  
agents

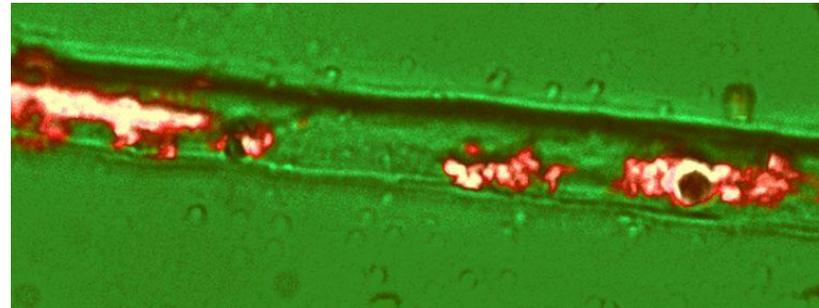
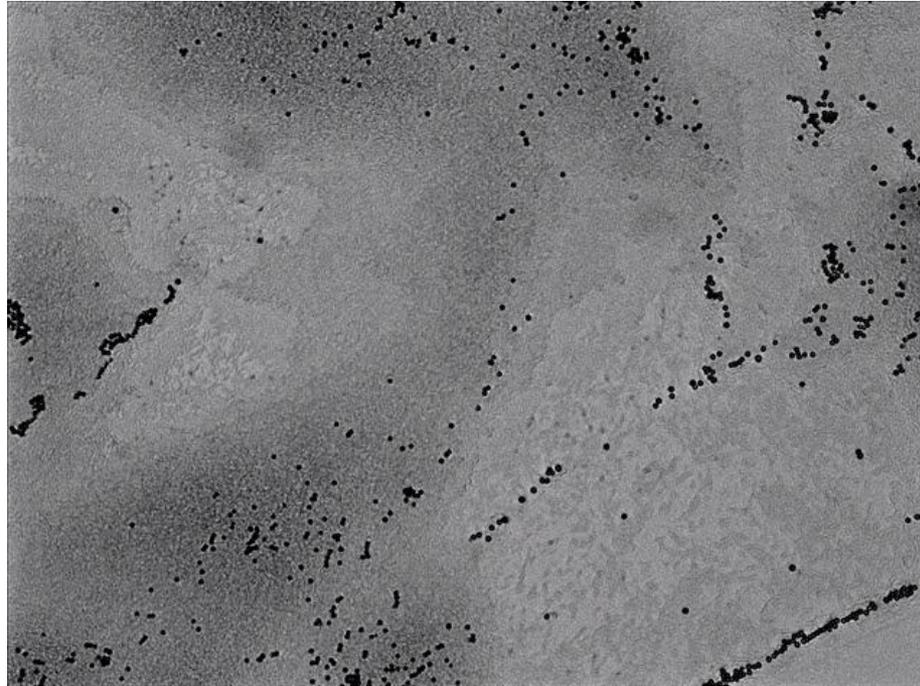
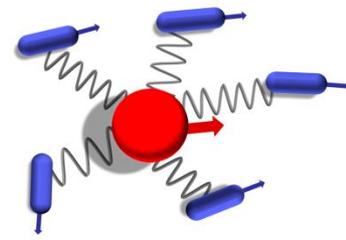
adaptable  
interactions



# Distribution of search paths



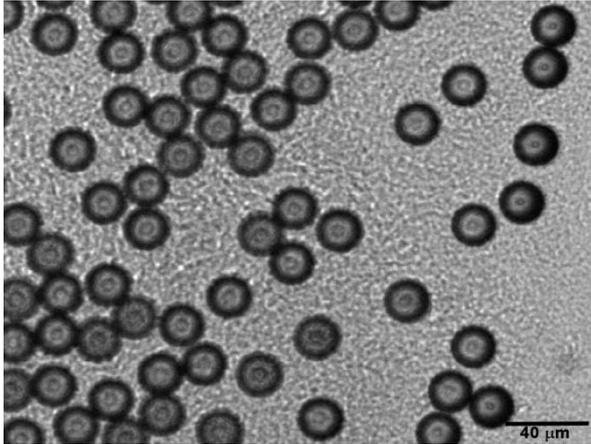
# Cargo Carrying Swarms



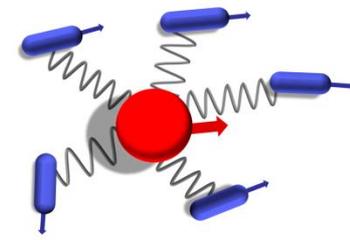
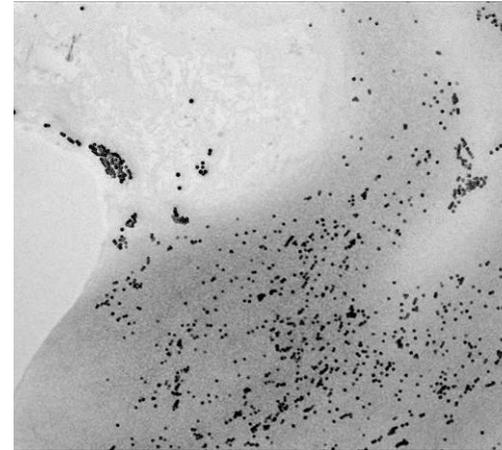
[Ingham *et al.* 2011, PNAS]

# Cargo Carrying Swarms

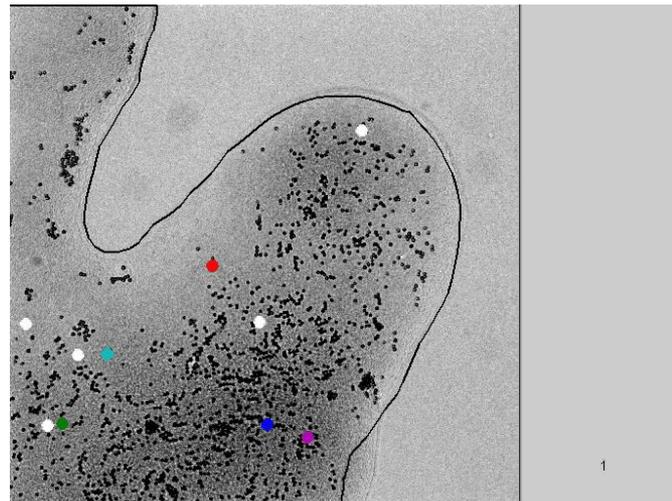
**Beads**



**Conidia**

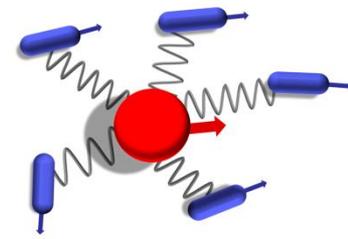


Bacteria swarms carry cargo and react to external forces

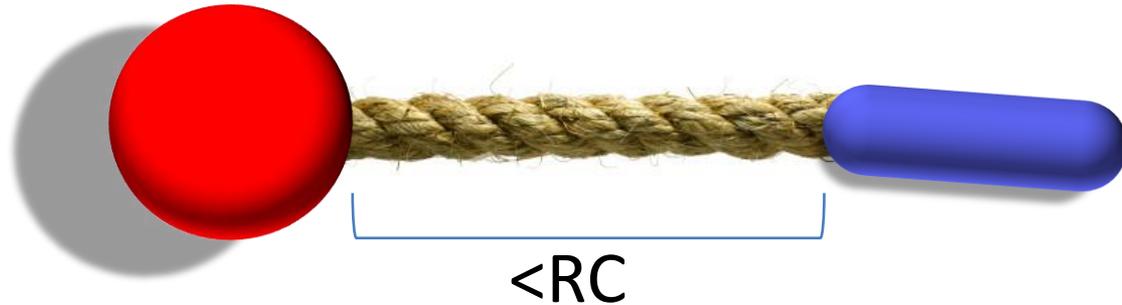


[Ingham *et al.* 2011, PNAS]

# Cargo Carrying Swarms



Rope Model:



$$\vec{v}_c(t+\Delta t) = \sum_{i \in RC_c(t)} \vec{b}_{ic}(t) \cdot \mathbf{k} + w \cdot \vec{v}_c(t)$$

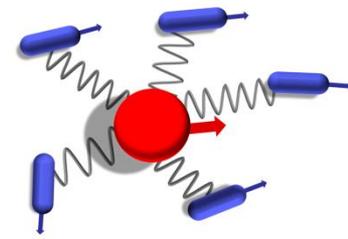
velocity direction

agent-cargo bond

constant force

previous velocity direction

# Cargo Carrying Swarms



Rope Model:



$$\vec{v}_i(t+\Delta t) = d_i(t) + \vec{b}_{ci}(t) \cdot \mathbf{k} + w \cdot \vec{v}_i(t)$$

velocity direction

group influence

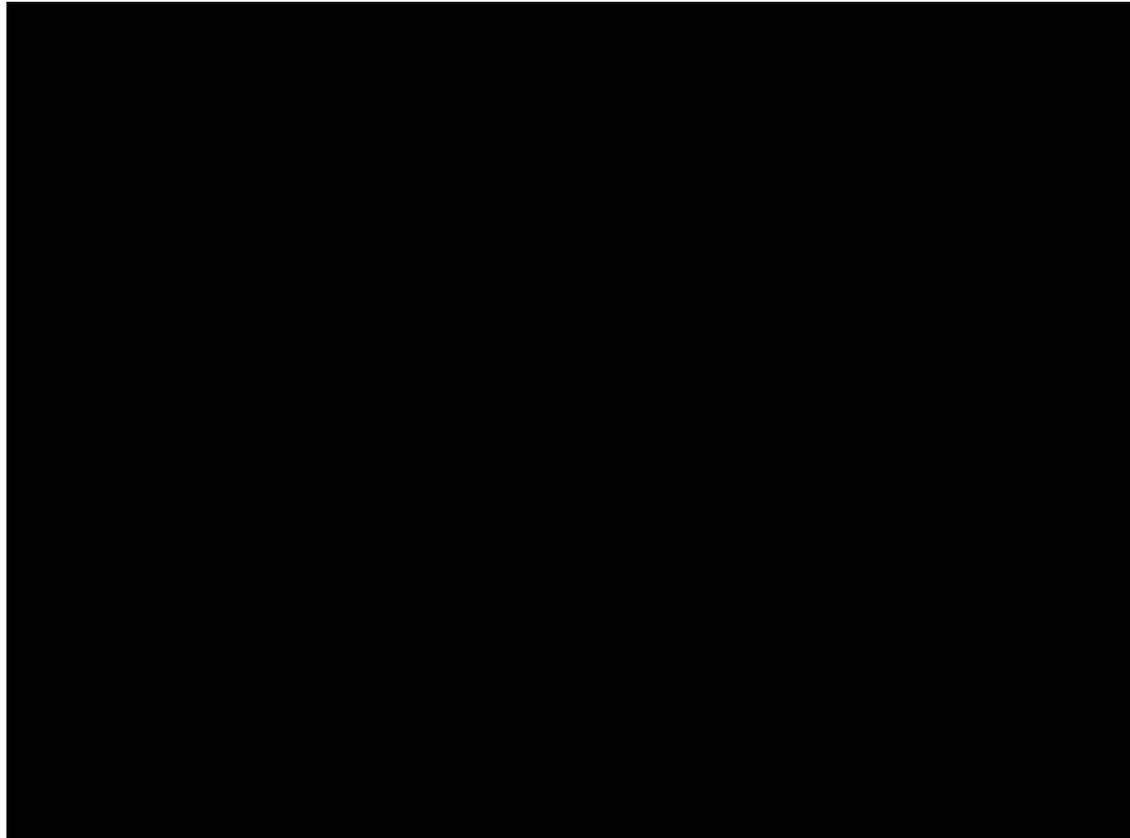
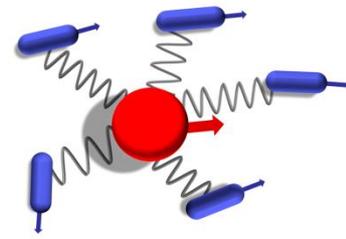
agent-cargo bond

constant force

previous velocity direction

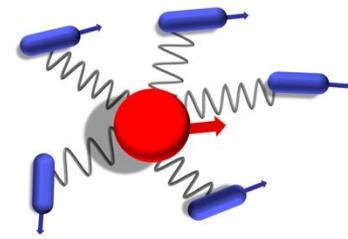
# Cargo Carrying Swarms

## Simulation of the rope model

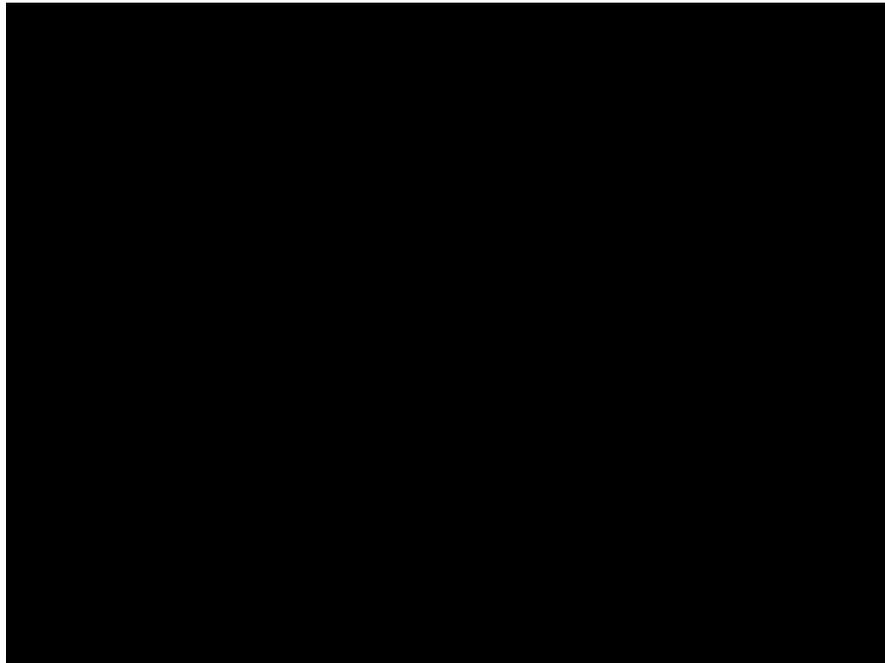




# Cargo Carrying Swarms

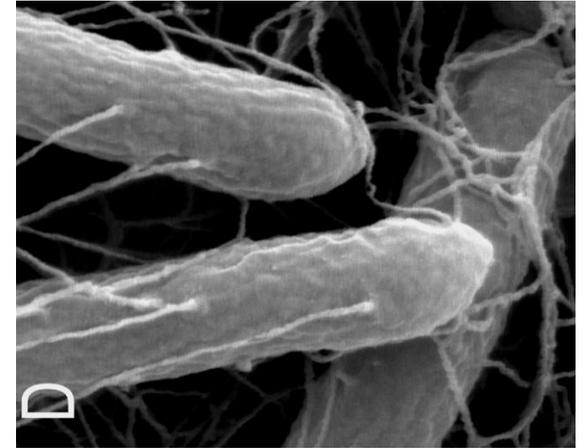
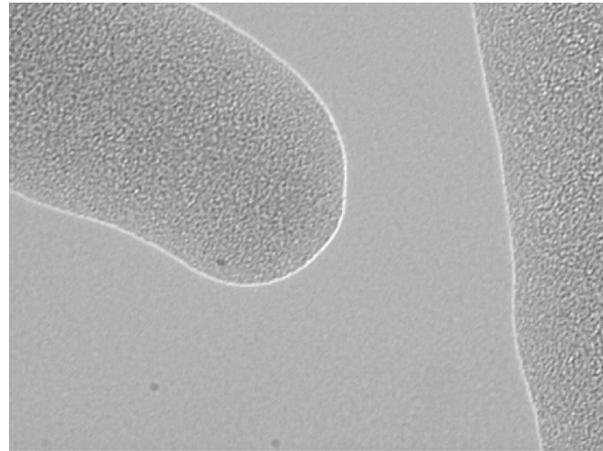


## Simulation of the extended model



Lubricating fluid edge is modeled as a discrete dual phase field  
Edge blocks motion of agents  
Enough close agents move the edge

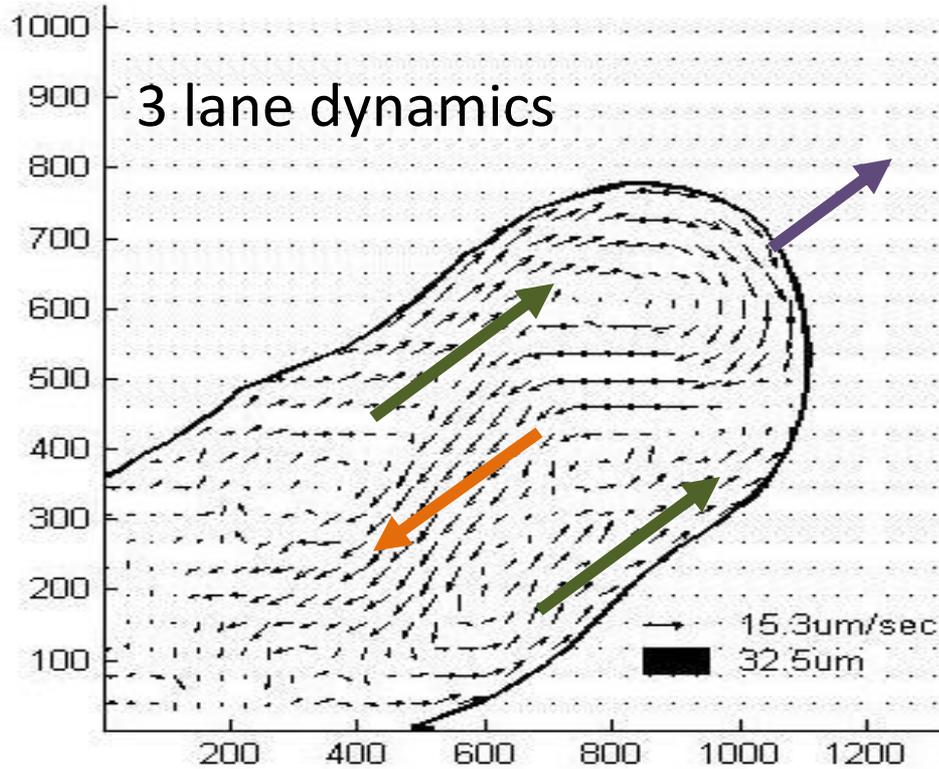
# Bacteria movement dynamics



Intermediate level: movement dynamics of a group of lubricating bacteria in an envelope

[pictures by Ingham and Ben-Jacob]

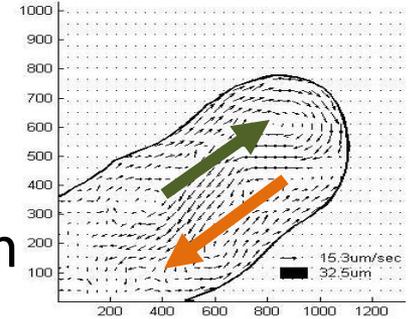
# Bacteria dynamics in a branch



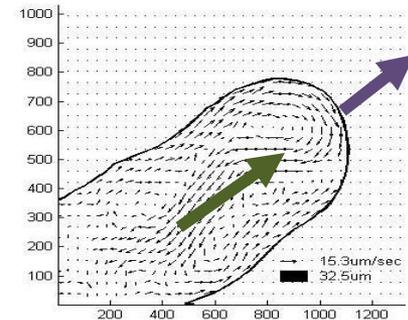
$$V_{\text{branch}} \approx \frac{3}{4} \cdot V_{\text{bacteria}}$$

constant branch width

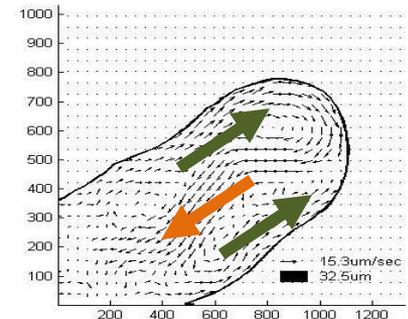
2 lane dynamics – static branch



1 lane dynamics

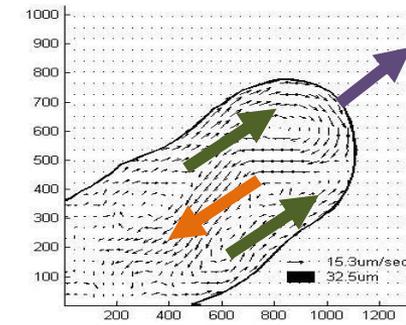
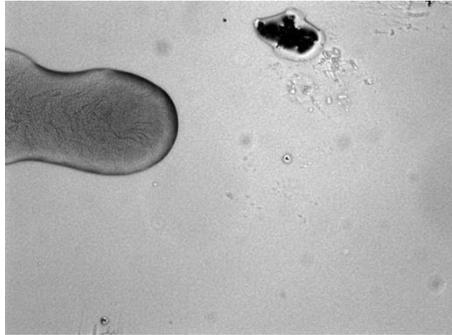


complex motion

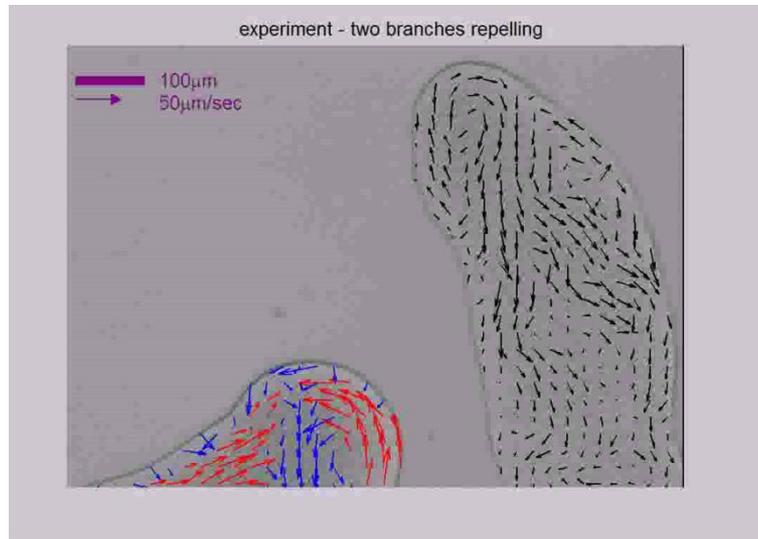


# 3 lane dynamics

collective  
chemotaxis



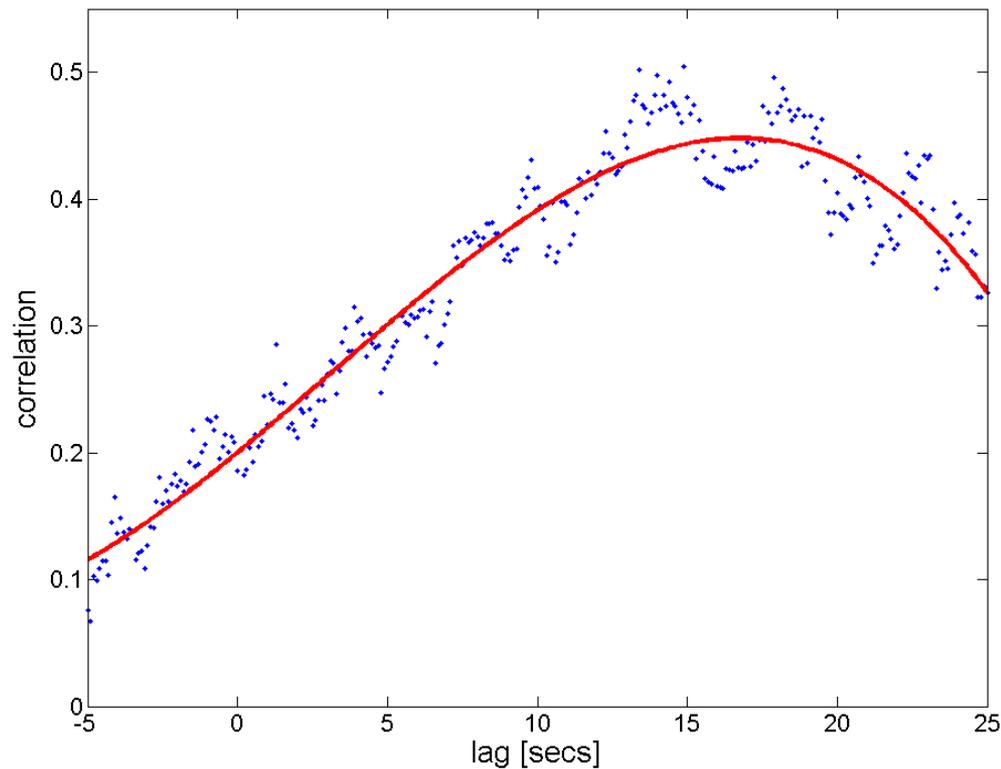
branch repulsion



[movie by Gil Ariel]

# Group navigation by collective organization

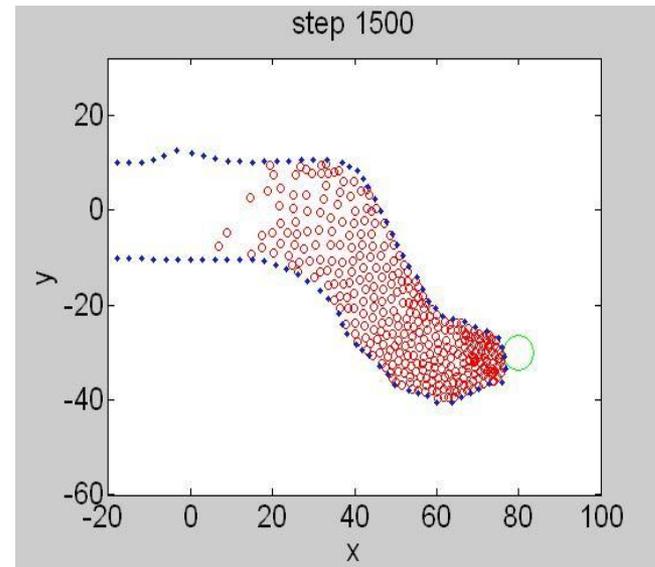
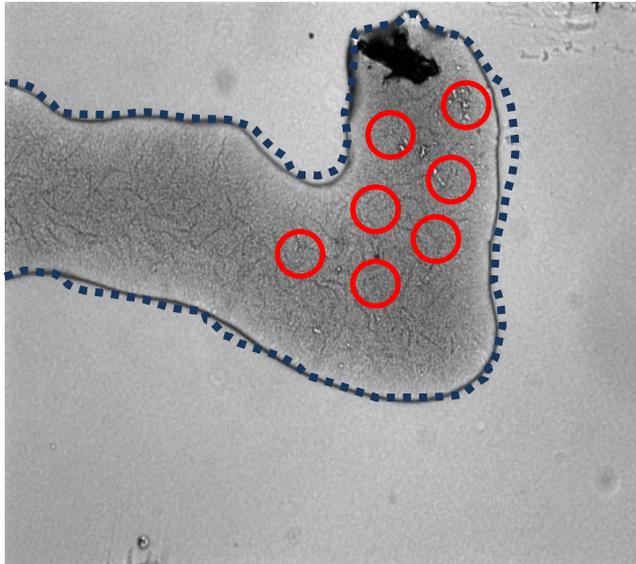
The point of return predicts the direction



[figure by Gil Ariel]

# Modeling branch dynamics

Identifying the key mechanisms underlying the dynamics

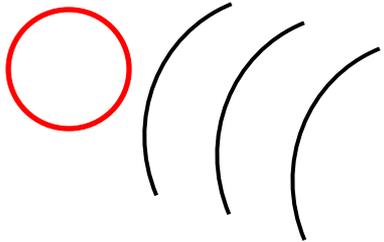


represents local cluster of bacteria -  
coarse graining of bacteria branch

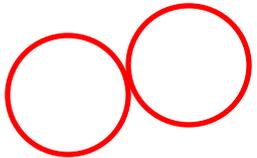


a dynamic boundary represents lubricating fluid limit

# Self propelled agents

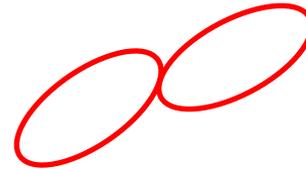


acceleration depends  
on attractant

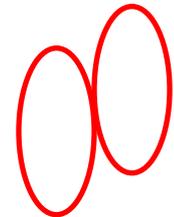


agent-agent  
interactions

Inelastic  
collisions



orientations

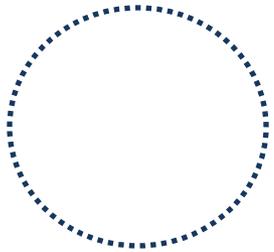


agent-envelope  
interactions

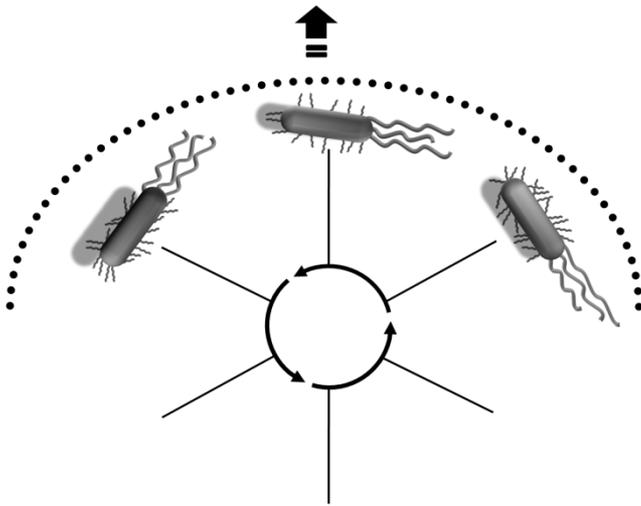
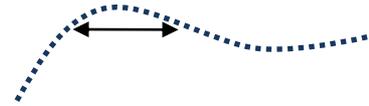
alignment



# Dynamic envelope



surface  
tension

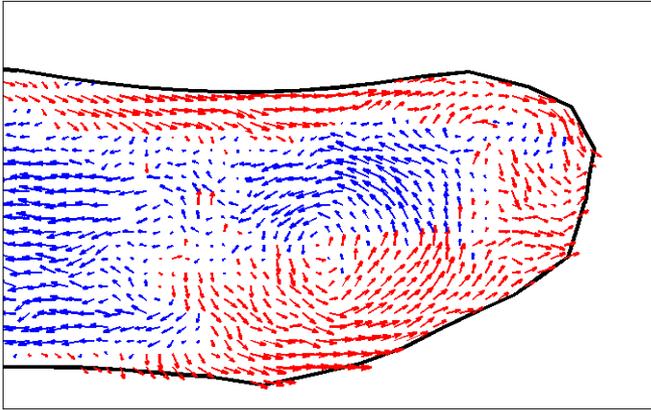


A phenomenological  
expression to the speed of  
the boundary

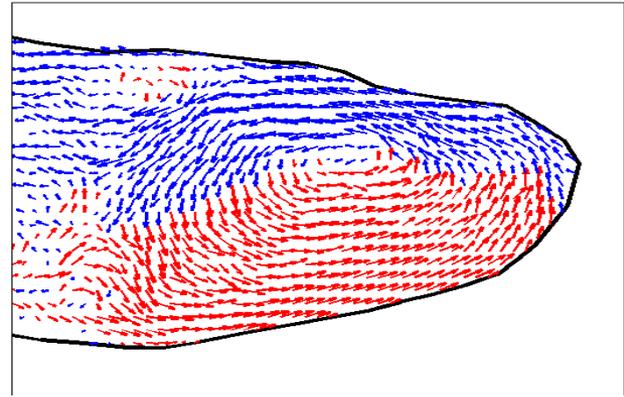
$$\frac{d\gamma_n(s)}{dt} \simeq \hat{v}_i \times v_i \times \nabla n$$

# Simulation

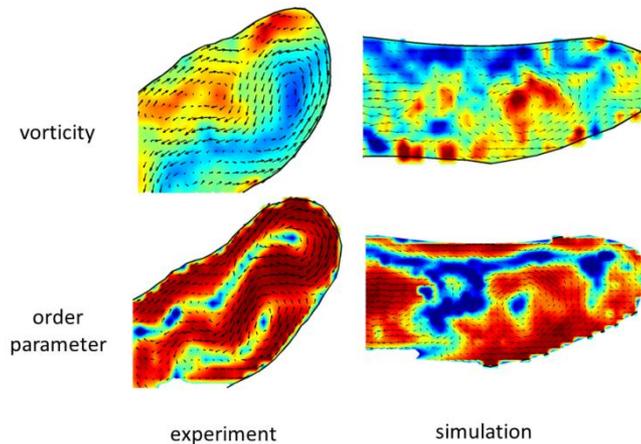
Moving branch with three lanes



Static branch with two lanes



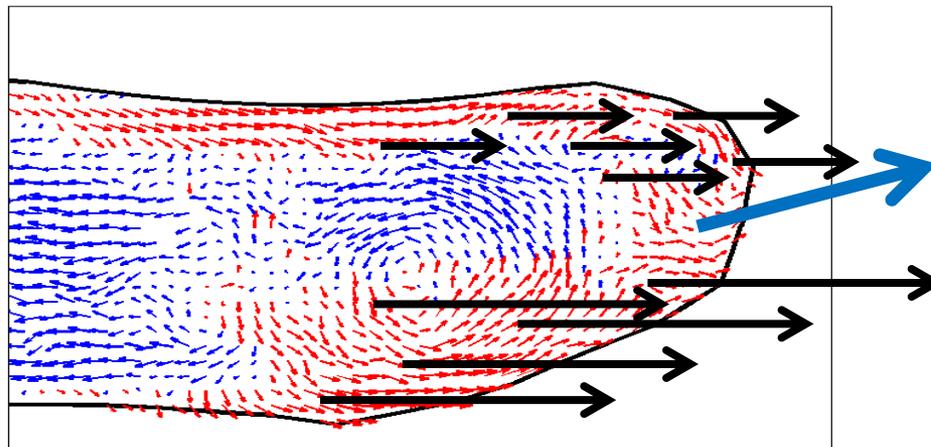
Agreement with experiments – velocity, vorticity, and order parameter



# How can local interaction rules control the direction of the branch?

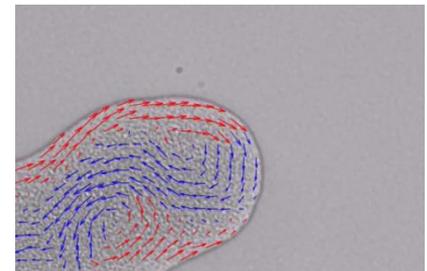
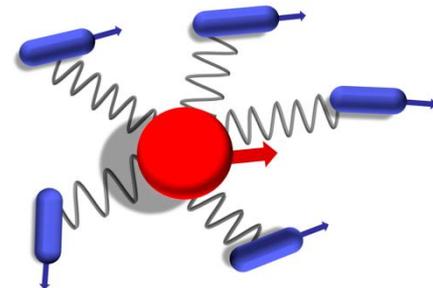
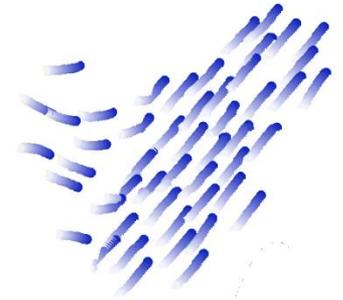
agents which become closer to the food source increase their speed

An uneven accumulation of cells on the side of the branch tip closer to the food source results in shifting of the tip to the other side



# Summary

- Adaptable interactions improve efficiency in a navigation task
- Complex behavior in cargo carrying swarms
- Navigation by self organization in bacteria branches



## Links:

- <https://sites.google.com/site/adishklarsh/>
- “Smart Swarms of Bacteria-Inspired Agents with Performance Adaptable Interactions”  
Shklarsh *et al.* PLoS Computational Biology
- “Collective Navigation of Cargo-Carrying Swarms”  
Shklarsh *et al.* Interface Focus