

We often learn elementary school math as a bunch of rules, without really understanding the concepts. Now that you're working on a higher level, a really good grasp of those basic ideas will help form a firm foundation for remembering the things you're encountering now.

If you understand how fractions (rational numbers) work, then working with rational expressions is much easier.

## FRACTIONS: What they are and why we have them

### JUST WHAT IS A FRACTION?

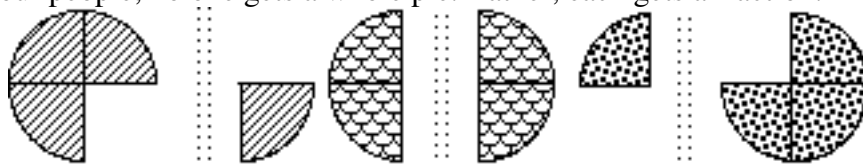
A fraction is a **part** of something. One half of a pie is *one* piece of a pie that has been cut into *two* pieces. In other words:

$$\frac{1}{2} \text{ is } \frac{\text{how many you have to work with}}{\text{how many are in a whole}} = \frac{(\text{numerator})}{(\text{denominator})}.$$

Two handy facts to keep in mind:  $\frac{\text{any number}}{\text{itself}} = 1$   $\left\{ \frac{a}{a} = 1 \right\}$  (You have all the pieces of the pie.)  
and  $\frac{\text{any number}}{1} = \text{itself}$   $\left\{ \frac{a}{1} = a \right\}$  (The pies are all in one piece.)

### FRACTIONS AND DIVISION

Fractions are really just another way of writing about and dealing with division. If I have three pies, and divide them equally among four people, no one gets a whole pie. Rather, each gets a fraction:



In the picture, each person has *three* pieces out of the *four* that each pie was cut into.

Mathematically, “3 pies divided among 4 people” is written as

$$3 \div 4 = \frac{3}{4} \quad (\text{or } \frac{3}{4}).$$

### KINDS OF FRACTIONS

In **proper** fractions the numerator is smaller than the denominator:  $\frac{3}{5}$ .

In **improper** fractions the numerator is larger than the denominator:  $\frac{5}{3}$ .

In **mixed numbers** there is a whole number part and a fraction part:  $1\frac{2}{3}$ .

(Once we get to algebra, and beyond, improper fractions are used rather than mixed numbers.)

### FINAL ENCOURAGEMENT

We deal with fractions all of the time, whether it's “two and a third cups” in a recipe, or knowing that 25 cents is a “quarter” of a dollar. Knowing what makes fractions tick is more than **half** the battle!